DEVELOPMENT AND MULTIPLE MODE CONTROL OF MODULAR AND RECONFIGURABLE ROBOT

by

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Development and Multiple Mode Control of Modular and Reconfigurable Robot Doctor of Philosophy 2013 Hongwei Zhang Aerospace Engineering Ryerson University

Abstract

There is a strong desire for robots to manipulate in uncontrolled environments. In uncontrolled environments, the robot has to adapt to the world consisting of only partially known or unknown objects and tasks, and real-time constraints. The capability of robots working in active or passive modes and switching between them helps enabling the robots to work in unstructured environments. Joint torque sensing is essential for implementing multiple mode control of robots. Though there have been a number of means of joint torque sensing, the existing joint sensing techniques have diverse limitations, such as in installation, reliability, cost, and noise immunity. This dissertation work develops a new joint torque sensing method for a modular and reconfigurable robot (MRR) with harmonic drive joints and provides solutions to multiple mode control of MRR based on the proposed sensing technique.

This research consists of two main parts. In the first part, a novel mathematical model for compliance of harmonic drives has been proposed. The proposed model captures not only the nonlinear stiffness but also the hysteresis phenomenon of harmonic drive transmission. Based on the developed harmonic drive compliance model, a joint torque estimation method using position measurements is developed. Torque estimation using position measurements provides an advantage of noise immunity to the estimated joint torque. Using the compliance of harmonic drives instead of an additional elastic component does not change the joint dynamics. Building upon the new torque estimation technique, a multiple working mode control algorithm for MRR is developed and experimentally validated.

The objective of the second part is to make the wrist suitable for dexterous manipulation in unstructured environments, such as door opening. A robust adaptive controller is developed for tracking control of the wrist in active mode; and a new interactive force compensation technique is proposed based on force sensor measurement, enabling passive working mode of the compact wrist without using mechanical solutions, which not only saves weight and volume, but also avoids losing tracking of the joints' position when switching from passive mode to active mode. Experiments on a prototype wrist have demonstrated the effectiveness of the proposed method.

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List of Symbols

- α Longitudinal angle
- β Latitudinal angle
- \ddot{q}_{mi}^{d} The desired joint-space motor side accelerations of the i_{th} joint
- δ Pitch angle
- \dot{q}_{mi}^d The desired joint-space motor side velocity of the i_{th} joint
- $\epsilon_{ri}, \epsilon_{Fij}$ positive control parameters

γ Yaw angle

- $\hat{b}_{mi}^c, \hat{f}_{mci}^c, \hat{f}_{msi}^c$ and $\hat{f}_{m\tau i}^c$ Estimations of the constant friction parameters of the i_{th} joint on motor side
- $\hat{ au}_{\delta}, \hat{ au}_{\gamma}$ the force/torque sensor measurements
- λ_i Controller parameter of the i_{th} joint
- μ_{Fic} positive constant
- ω_c Harmonic drive circular spline angular velocity
- ω_{fi} Harmonic drive flexspline input angular velocity
- ω_f Harmonic drive flexspline angular velocity
- ω_i Joint velocity of the *i*th joint
- ω_w Harmonic drive wave generator angular velocity

 ϕ Incline angle

 Ψ Harmonic drive hystersis loss

 $\rho_{\alpha_{base}}$ The bound of acceleration associated with motion of the base

 $\rho_{\tau\delta}, \rho_{\tau\gamma}$ bounds of the force/torque sensor measurement error

 $\rho_{\tau_{ti}}$ The bounds of torque measuring error of the *i*th joint

 $\rho_{F_{mi}}$ The bound of F_{mi}

 $\rho_{f_{qmi}}$ The bound of f_{qmi}

 ρ_{Fi} Constant bound of F_i^v

- ρ_{fqi} Constant bound of nonparametric friction
- τ_{α} Torque along longitudinal direction
- τ_{β} Torque along latitudinal direction
- τ_{δ} Torque along pitch direction
- τ_{γ} Torque along yaw direction
- τ_{basei} The inertial and Coriolis forces of the *i*th joint
- τ_c Torque at harmonic drive circular spline
- τ_{exti} External torque added to link of the *i*th joint
- au_{fb} Harmonic drive back-driving torque
- au_{fr} Harmonic drive friction torque
- au_{fs} Harmonic drive starting torque
- τ_f Torque at harmonic drive flexspline
- τ_i Joint torque of the *i*th joint

- τ_{kerr} Estimated torque error caused by kinematic error
- τ_{mi} Motor output torque of the *i*th joint
- τ_{ti} Torque transferred at transmission system of the *i*th joint
- τ_w Torque at harmonic drive wave generator
- θ_c Harmonic drive circular spline position
- θ_{errl} Kinematic error component related to link position
- θ_{errw} Kinematic error component related to motor position
- θ_{err} Harmonic drive kinematic error
- θ_{fi} Harmonic drive flexspline input position
- θ_{fo0} Flexspline position at first index after power on
- θ_{fo} Harmonic drive flexspline output position
- $\theta_{fo}^{cw_i}$ Flexspline position while index come at clockwise free run
- $\theta_{fo}^{cw_i}$ Flexspline position while index come at count-clockwise free run
- θ_f Harmonic drive flexspline position
- θ_{IE} Motor-side incremental encoder reading
- θ_i Joint position of the *i*th joint
- θ_{offset} Motor-side incremental encoder offset
- θ_{wi} Harmonic drive wave generator input position
- θ_{wo} Harmonic drive wave generator output position
- θ_w Harmonic drive wave generator position
- $\triangle \theta$ Harmonic drive deformation

- $\triangle \theta_f$ Harmonic drive flexspline deformation
- $\triangle \theta_w$ Harmonic drive wave generator deformation
- $a_0, a_{l1}, b_{l1}, w_l, a_{w1}, a_{w2}, b_{w1}, b_{w2}, w_w$ Parameters for kinematic error modeling
- a_1, a_2 Harmonic drive stiffness constants
- b_i Viscous friction coefficient for the *i*th joint
- b_{li}, b_{mi} The viscous friction coefficients of the *i*th joint
- $C_{\alpha} = \cos \alpha$

 $C_{\beta} = \cos \beta$

 $C_{\delta} = \cos \delta$

- $C_{\gamma} = \cos \gamma$
- $C_{\phi} = \cos \phi$
- $C_i \qquad \cos \theta_i$
- c_f Harmonic drive flexspline stiffness nolinear constant
- *F* Force added to spring system
- F_a Force added to spring a
- F_b Force added to spring b
- $F_i \qquad [b_i f_{ci} f_{si} f_{\tau i}]^T$

 $f_i(q_i, \dot{q}_i)$ the friction of the *i*th joint

 F_i^c Constant part of F_i

 F_i^v Variable part of F_i

 $F_x, F_y, F_z, \tau_x, \tau_y$ and τ_z Measurements of the force/torque sensor

- $f_{\tau i}$ Parameter corresponding to the Stribeck effect for the *i*th joint
- f_{ci} Coulomb friction related parameter for the *i*th joint
- F_{fr} Friction force
- $f_{l\tau i}, f_{m\tau i}$ Parameters corresponding to the Stribeck effect of the *i*th joint
- f_{lci}, f_{mci} The Coulomb friction-related parameters of the *i*th joint
- $f_{li}(q_{li}, \dot{q}_{li})$ Joint friction of the *i*th joint on link side
- f_{lsi}, f_{msi} The static friction friction-related parameters of the *i*th joint

$$F_{mi} \quad [b_{mi} f_{mci} f_{msi} f_{m\tau i}]^T$$

- $f_{mi}(q_{mi}, \dot{q}_{mi})$ Joint friction of the *i*th joint on motor side
- F_{mi}^c The constant part of F_{mi}

$$F_{mi}^v$$
 The variable part of F_{mi}

 f_{qli}, f_{qmi} The friction modeling errors of the *i*th joint

- f_{si} Static friction related parameter for the *i*th joint
- $g_{li}(q_{l0}...q_{li})$ Link gravity of the *i*th joint
- I_{li} Moment of inertia of the *i*th link about the axis of rotation
- I_{mi} Moment of inertia of the *i*th rotor about the axis of rotation
- J_c, J_2 Jacobian matrixes
- K_1, K_2, K_3 Harmonic drive stiffnesse segments
- K_{f0} Harmonic drive flexspline initial stiffness
- K_{fl} Harmonic drive flexspline local stiffness
- K_{pi} The control parameter used for passive mode

K_{w0}, α	w_w Wave generator stiffness factors
K_{wl}	Wave generator local stiffness

- N Harmonic drive gear ratio
- N_i Reduction ratio of the speed reducer of the *i*th joint
- q_{li} Link position of the *i*th joint
- q_{mi} Motor position of the *i*th joint
- q_{mi}^d The desired joint-space motor side position the i_{th} joint
- $S_{\alpha} = \sin \alpha$
- $S_{\beta} = \sin \beta$
- $S_{\delta} = \sin \delta$
- $S_{\gamma} = \sin \gamma$
- $S_{\phi} = \sin \phi$
- $S_i \quad \sin \theta_i$
- t_s The time for the solution trajectory
- T_1, T_2 Harmonic drive Split torque
- t_{ij} Elements of transform matrix

 T_{ij}, T_{ijs}, T_{im} Transform matrixes

V The Lyapunov function candidate

X Total displacement

- z_{li} Unity vector along the axis of rotation of the *i*th link
- z_{mi} Unity vector along the axis of rotation of the *i*th joint

Chapter 1

Introduction

The purpose of this chapter is to provide the background information and to introduce some underlying materials related to the dissertation. Furthermore, it presents the objective and contribution of the dissertation work. At the end of this chapter, an organization outline for the remainder of the dissertation is presented.

1.1 Manipulation in Uncontrolled Environment

Robots have long been desired to get closer to human beings, to help us in daily lives, to work alongside us, to provide physical assistance on an assembly line or to help us with household chores. Traditional manipulators are mostly position controlled with fixed configuration and joints working in a single active mode. Such manipulators have been successful in controlled environments such as in a production line of a factory. Outside of controlled (structured) environments, they perform sophisticated manipulation tasks only when operated by human operators. It is time now for robots to move beyond structured factory settings, where they have made great success, into environments populated with people, to co-exist and cooperate with their human owners. Human environments pose a significant challenge for robotic manipulation because of their complexity and inherent uncertainty (Kemp et al. 2007). The conventional industrial manipulators with position control are unsuitable for sophisticated manipulation in human environments (Liu et al. 2008); and the development of robots capable of working in unstructured human environments has become the trend of technology advancement of robotics. As one of the most omnipresent artificial environments, doors represent a serious challenge

for robots; and door-opening has attracted the attention from numerous researchers (Nagatani and Yuta 1996; Petersson et al. 1997; Niemeyer and Slotine 1997; Khatib 1999; Liu et al. 2009). A high-level control approach using off the-shelf force/torque control algorithms was developed for door-opening with mobile manipulators (Petersson et al. 1997). A general door-opening strategy was proposed on the basis of action primitives, and the approach was validated by experiments on a mobile manipulator (Nagatani and Yuta 1996). Simultaneous control of mobile platform and the onboard manipulator was investigated for a mobile manipulator opening a door (Khatib 1999). To solve the door-opening problem, a relatively simple control method was proposed by following the path of least resistance (Niemeyer and Slotine 1997). Recently in our lab, a door opening algorithm was developed using modular and reconfigurable robots (Liu et al. 2009). More recently in our lab, a door opening algorithm is developed for mobile manipulators, which integrates a mobile platform with an onboard manipulator, and multiple mode control of the onboard manipulator is essential for performing the door-opening task (Ahmad and Liu 2010).

Robotic passivity has long been identified to be a useful characteristic for cooperative control of multiple manipulators (Liu et al. 1999). For manipulation in unstructured environments such as door opening, it is desirable to grasp the door knob with active position control and to pull the door open with selected joints working in a passive working mode. To implement the passive mode, several algorithms have been proposed, including the one based on friction compensations (Liu et al. 2008), and another approach based on torque sensor feedback (Ahmad and Liu 2010). Both of them are for general rotary joints and with some limitations. For instance, the friction compensation based method works only when the motion trend is known.

For developing robot manipulators working in human environments, a light weight and compact wrist joint is extremely desirable. A compact wrist has been designed and fabricated in our laboratory based on the serpentine robot joint (Paljug et al. 1995) and double active universal joint (Ryew and Choi 2001), which has a compact mechanism with two degrees of freedom. However, it is difficult to integrate joint torque sensors into the wrist, which is equipped with position sensors only. In this dissertation research, a multiple mode control algorithm is proposed for the control of the compact wrist based on a wrist force senor which enables online switching between an active position control mode and a passive interactive force compensation mode of the wrist.

1.2 Harmonic Drive Compliance Model

Harmonic drives, invented in 1950s (Musser 1955), are widely used in servo systems, such as robots, due to their desirable characteristics of near-zero backlash, compactness, light weight, high torque capacity, high gear ratio and coaxial assembly. In the meantime, a number of attempts have been made towards the analytical modeling of harmonic drives. Volkov and Zubkov (1978) pioneered the investigation of harmonic drive transmission dynamics incorporating stiffness. During the mid/late-1980s, Good et al. (1985) and Kojima et al. (1989) investigated the effects of the harmonic drive on robotic systems dynamic control. Empirical data were used to show that performance degradation occurs if the joint flexibility is ignored in controller design of robot manipulators (Good et al. 1985). The effect of nonlinear friction of harmonic drive transmissions on robotic systems performance was studied (Kojima et al. 1989). Marilier and Richard (1989) modeled the harmonic drive behavior including factors like nonlinear stiffness, backlash, and nonlinear friction torque. Hidaka et al. (1990) reported the effects of transmission compliance and kinematic error on vibration during operation. In the existing literature, it has been a common observation that the aggregated effects of compliance, hysteresis, and kinematic error take part in the dynamics of harmonic drive transmission systems (Schempf and Yoerger 1993; Kircanski and Goldenberg 1997). However, accurate modeling of the harmonic drive transmission system remains a challenging task. The majority of existing models are either too complicated with the difficulty to estimate parameters, or over simplified without incorporating the nonlinear stiffness and hysteresis. Some proposed hysteresis models require the derivative of torsional angle, which is impractical to obtain because of measurement noise. For instance, Dhaouadi and Ghorbel (2003) introduced a mathematical hysteresis model based on ferromagnetic hysteresis study. Tjahjowidodo et al. (2006) described the dynamics of harmonic drives using nonlinear stiffness characteristics combined with distributed Maxwell-slip elements that capture the hysteresis behavior. Curt et al. (2012) recently provided a more comprehensive hysteresis model. However, these models are complicated and require the derivative of torsional angle, using model parameters that are difficult to estimate.

In the previous works, the harmonic drive models are formulated by modeling each of its individual behaviors and then incorporating these models into equations governing the harmonic drive transmission. The downside of such an approach is the complexity of model(s), which stems from the complexity of behavior, with nonlinear torsional compliance and hysteresis being on top of the list. In this dissertation, the proposed model is derived by modeling the compliance of each component of the harmonic drive instead of modeling its individual behavior. Subsequently, the resulting model can capture the harmonic drive behaviors without using complicated hysteresis or kinematic error models. Furthermore, the proposed model does not require the derivative of the torsion angle. The harmonic drive transmission system model is derived in two sequential steps: in the first step, a model for the compliance of each individual component is derived; in the second step, a complete harmonic drive model, capturing both the nonlinear compliance and hysteresis, is obtained by a synergetic integration of the individual models.

1.3 Joint Torque Sensing

Joint torque feedback (JTF) has been widely recognized to improve the performance of robot control in the robotics community (Aghili et al. 2001; Liu et al. 2006; Zhu et al. 2007; Tien et al. 2008). The JTF is used in robot control to suppress the effect of load torque on motion control (Aghili et al. 2007). The use of joint torque sensors can significantly relax the need to model the link dynamics. Dynamic control of robots can then be performed by joint torque sensing feedback without computing inverse dynamics of robots. Joint torque sensing is also valuable in force, compliance, and impedance control. In addition, joint torque sensing is necessary for collision detection and reaction.

In order to apply JTF, it is necessary to measure or estimate the transmitted torque by the harmonic drive transmission. Conventionally, to implement such control strategies, the robot is equipped with joint torque sensors or a multi-axis force/torque (F/T) sensor. When using F/T sensor at the robot wrist, the estimation of joint torques requires additional calculations, and the results may be affected by computation delays and model errors (Randazzo et al. 2011). Furthermore, the commercially available torque sensors are costly and need extra space and mechanical modification to the joints.

There are several techniques of direct joint torque sensing, e.g., joint torque sensors based on elastic elements that are placed in the output transmission line of each joint of the robot (Vischer and Khatib 1995; Tsetserukou et al. 2006). However, for robotic joints with harmonic drive transmission, which has an elastic flexspline, and an additional compliant element may compromise the joint stiffness. Vischer et al. (1995) and Tsetserukou et al. (2006) measure deformation of an elastic body after the reduction mechanism with optical distance sensors. Kawakami et al. (2010) used a linear encoder to measure the torsional deformation of the additional elastic body. As measurement accuracy is in inverse proportion to sensor stiffness, low sensor stiffness is inevitable in order to achieve high measurement resolution, which leads to complicated joint dynamics. The additional elastic component also affects the link position measurement accuracy.

Another joint torque sensing technique is based on the method proposed by Hashimoto et al. (1993). Joint torque sensing is achieved by mounting strain gages directly on the harmonic drive, which is usually referred to as built- in torque sensing for harmonic drives (Hashimoto et al. 1993; Taghirad and Belanger 1998; Godler et al. 2000). The torsional compliance of harmonic drives lends itself to torque sensing, but the elliptical shape of the wave generator in harmonic drive transmissions introduces a spatially dependent local torque ripple on the flexspline of harmonic drives. It is difficult to extract the applied torque signal from this local torque ripple if the applied torque is sensed at the flexspline of the harmonic drive (Sensinger and Weir 2006).

In recent years, high resolution absolute position encoders become commercially available. This makes it possible to measure the torsional deformation of harmonic drive. In this dissertation, a joint torque estimation method based on a harmonic drive compliance model is developed. The torsional deformation of the harmonic drive is measured using link-side encoder and the resulted measurement is used with the proposed harmonic drive compliance model to estimate the joint torque. The proposed torque estimation method is economical and represents an effective way of torque estimation for robots with harmonic drives.

1.4 Multiple Mode Control

In order to adapt various tasks, sometimes the robot joints have to work in a passive mode. In the relevant published literature, passive joints are used in the cooperation control of multiple manipulators (Li et al. 2007; Nung et al. 2001; Liu et al. 1999). In reference (Nung et al. 2001), the motion planning and control of mobile manipulators are greatly simplified by using the exchangeable active/passive joints, where the positioning error of the mobile manipulator can be absorbed passively and detected as the angular information of passive joints. Relatively complex tasks are executed without using external sensors such as a vision or a wrist force

sensor.

Robot manipulators with passive impedance based on mechanical compliances have been investigated by many researchers. Design of robot joints with programmable passive impedance using antagonistic nonlinear springs and binary dampers was studied in reference (Laurin-Kovitz et al. 1991). Passive impedance control using viscoelastic material and a passive trunk mechanism was developed in reference (Suita et al. 1995). A mechanical impedance adjuster was reported in reference (Iwata et al. 1999) and (Morita and Sugano 1996), where a variable spring and damper adjusted by an electromagnetic brake were used for a passive compliant joint.

A recent hybrid joint was developed in references (Li et al. 2007; Li et al. 2004; Luo et al. 2006), which introduces an electromagnetic clutch between the motor and the output shaft. This hybrid joint has both the passive and active working modes. When the clutches are released, the joints are free and passively controlled by the coupling forces of a manipulator. The joint is capable of compliantly adapting to external force and motion by switching between the active and passive modes depending on the requirement of the given task. However, this hybrid joint needs a recovering algorithm to resume the joint position.

All of the hybrid active/passive joints or mechanisms mentioned above have to be specially designed, which leads to extra weight and volume due to the additional components. In some cases, passive joints can help reduce power consumption, increase flexibility, and improve safety. It is desirable to be able to switch a normal robot joint to a passive operation mode without changing the existing joint mechanism or electronics system. For example, robot-mediated motor therapies have been widely investigated in rehabilitation robots recently (Krebs et al. 1998; Burgar et al. 2000; Lum et al. 2002; Colombo et al. 2006). A robotic therapy allows subjects to perform voluntary movements, thus promoting neurogenesis and neuroplasticity, and optimizing the functional recovery after neurological injuries (Schaechter 2004; R. Teasell and Bitensky 2005), This means that the rehabilitation robots have to provide assistance as needed, so that not to perturb voluntary movements of the users, and to help completing the tasks that they are not able to perform autonomously. In this sense a passive ability during a retrograde motion, is of crucial importance.

In this dissertation, building upon the new torque estimation technique, a multiple working mode control algorithm for modular reconfigurable robot rotary joint is developed. Also a multiple mode control system of a compact wrist is developed. The passive mode is realized without using mechanical solutions such as a clutch, which not only saves weight and volume

of the joint, but also avoids losing track of the joints' position when switching from passive mode to active mode. These make the modular reconfigurable robot suitable for dexterous manipulation in unstructured environments, such as door opening.

1.5 Publications

1.5.1 Journal Papers

- 1. H. Zhang, Y. Liu, and G. Liu, "Multiple Mode Control of a Compact Wrist with Application to Door Opening," Mechatronics, Vol.23, No.1, Pages 10-20, Feb., 2013.
- S. Ahmad, H. Zhang, and G. Liu, "Multiple Working Mode Control of Door Opening with a Mobile Modular and Reconfigurable Robot," IEEE/ASME Trans. on Mechatronics, Vol.18, No.3, Pages 833-844, Jun., 2013.
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1.5.2 Conference Papers

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1.6 Organization of Dissertation

This dissertation consists of seven chapters and is organized as follows. Detailed literature reviews and background information are given in the first chapter. Chapter 2 focuses on harmonic drive compliance model. A novel mathematical model for the compliance of harmonic drives is presented in this chapter. Combined with a simple friction model, the proposed model captures the nonlinear stiffness and hysteresis phenomenon of harmonic drive transmission. Numerical simulations and experiments have been used to test the proposed model. In Chapter 3, a joint torque estimation method based on position measurement is presented along with a new harmonic drive compliance model. Torque estimation based on position measurements provides an advantage of noise immunity to the estimated joint torque. Using the torsional compliance of harmonic drives instead of an additional elastic component does not change the joint dynamics. Moreover, adding a link-side position sensor has the potential to improve joint control accuracy and reduce the cost of joint torque sensing. In this chapter, three sets of experiments are conducted and the results are reported. In Chapter 4, by using the estimated torque, a multiple mode control method is developed for MRR robot joint, making it work in an active mode with position control, or a passive mode with friction compensation. A robust adaptive control algorithm is developed for motion control of MRR in the active mode; and an friction compensation technique is proposed to make it capable of working in the passive mode. Active and passive mode experiments are also reported in this chapter. Chapter 5 presents the anthropomorphic wrist mechanical design and analysis. In the first section, mechanical design is reviewed, and motion analysis is also provided in this section. The kinematic analysis is given in the second section. In the last section, inverse kinematics, differential kinematics and force analysis are presented. In Chapter 6, a multiple mode control method is developed for the compact wrist, making it work in the active mode with position or torque control, or the passive mode with interactive force compensation. A robust adaptive control algorithm is developed for motion control of the compact wrist in active mode; and an interactive force compensation technique is proposed to make it capable of working in passive mode. Experiments in both the active and passive modes are provided. An application in door opening is described in the end of this chapter. Final conclusion and future research discussions are provided in Chapter 7.

Chapter 2

Compliance and Hysteresis Model of Harmonic Drive

2.1 Mechanism of Harmonic Drive

A typical harmonic drive consists of three main components as shown in Fig. 2.1 (Harmonic Drive LLC 2012): the wave generator (WG) connected to a motor, the circular spline (CS) connected to the base, and the flexspline (FS) sandwiched in between CS and WG and connected to the joint output.



Figure 2.1: Exploded view of a harmonic drive showing the three components

The WG is composed of an elliptical disk (rigid elliptical inner-race), called wave generator

plug, and an outer ball bearing, both of which are separate parts. The wave generator plug is inserted into the bearing, thereby giving the bearing an elliptical shape as well. The FS fits tightly over WG; when the WG plug is rotated, the FS deforms and molds into the shape of the rotating ellipse but does not rotate with the WG.

2.2 Harmonic Drive Model

2.2.1 Basic Model



Figure 2.2: The basic kinematic representation of a harmonic drive

The kinematic relationship, explained in (Harmonic Drive LLC 2012), equates the angular positions at the three parts of the harmonic drive

$$\theta_w = (N+1)\,\theta_c - N\theta_f \tag{2.1}$$

where, N denotes the gear ratio, θ_w , θ_c , and θ_f refer to the angular positions of the wave generator, the circular spline, and the flexspline, respectively. These are also illustrated in Fig. 2.2. Taking the derivative of Eq.(2.1) with respect to time results in Eq.(2.2), an expression

in terms of the angular velocity

$$\omega_w = (N+1)\,\omega_c - N\omega_f \tag{2.2}$$

where ω_w , ω_c , and ω_f denote the corresponding angular velocities. The static force balance between the elements can be established as

$$\tau_w = \frac{1}{(N+1)}\tau_c = -\frac{1}{N}\tau_f$$
(2.3)

where τ_w , τ_c , τ_f represent the torque at the wave generator, circular spline, and flexspline, respectively. To be consistent with the existing literature and general existing applications, where the circular spline is usually fixed, so that $\theta_c = 0$ and $\omega_c = 0$, and we are unconcerned with the circular spline reaction torque τ_c . Therefore, Eq.(2.1) to Eq.(2.3) can be simplified as

$$\theta_w = -N\theta_f \tag{2.4}$$

$$\omega_w = -N\omega_f \tag{2.5}$$

$$\tau_w = -\frac{1}{N}\tau_f. \tag{2.6}$$

The basic model mentioned above captures the harmonic drive's ideal linear input/output relationship. For example, the harmonic drive transmission is treated as a perfectly rigid gear reduction mechanism. The empirical measurements of the input/output relationship provided in the cited literature clearly show that the output is not linearly related to the input (Curt et al. 2012). The causes of this nonlinearity are compliance in the harmonic drive parts, nonlinear viscous friction, and the kinematic error due to gear meshing. This fact motivated the need for a more comprehensive harmonic drive model.

2.2.2 Basic Model with Compliance and Friction

In this harmonic drive model, both the compliance of flexspline and the harmonic drive friction are considered. Other aspects of the harmonic drive behaviour such as, hysteresis, wave generator compliance, kinematic error, and nonlinearity are neglected. These are also illustrated in



Fig. 2.3. The classic compliance model is described by Eq.(2.7) to Eq.(2.9).

Figure 2.3: The kinematic representation of a harmonic drive showing flexspline compliance

$$\theta_w = -N\theta_{fi} \tag{2.7}$$

$$\omega_w = -N\omega_{fi} \tag{2.8}$$

$$\tau_w = -\frac{1}{N}(\tau_f - \tau_{fr}) \tag{2.9}$$

where τ_{fr} is the friction torque; θ_{fi} and ω_{fi} denote the flexible spline position and velocity at flexspline gear-side (flexspline gear-toothed circumference), respectively. As described in a manufacturer's catalogue (Harmonic Drive LLC 2012), the typical shape of the stiffness curve possesses two characteristic properties: increasing stiffness with displacement and hysteresis loss. To capture this nonlinear stiffness behavior, the manufacturers suggest using piecewise linear approximations (Harmonic Drive LLC 2012), whereas several independent researchers prefer a cubic polynomial approximation, i.e., as in (Volkov and Zubkov 1978; Hidaka et al. 1990), the nonlinear flexspline output torque, τ_f , was approximated by a third order polynomial function of the torsion angle as

$$\tau_f = a_1 \triangle \theta + a_3 (\triangle \theta)^3 \tag{2.10}$$

where $\triangle \theta$ is harmonic drive torsion angle, the difference between harmonic drive real output and ideal output, a_1 and a_3 are the constants to be determined.

Remark 1 The approximation of the nonlinear flexspline output torque by a cubic polynomial Eq.(2.10) is not convenient for control purposes as in most control applications, τ_f is available (measured) and $\Delta \theta$ needs to be calculated.

Another method of estimating the torsion angle is described in (Harmonic Drive LLC 2012), where $\Delta \theta$ was approximated by a piecewise linear function of the output torque as shown Fig. 2.10.

$$\Delta \theta = \begin{cases} \frac{\tau_f}{K_1} & \tau_f \leq T_1\\ \frac{\tau_1}{K_1} + \frac{(\tau_f - T_1)}{K_2} & T_1 < \tau_f < T_2\\ \frac{\tau_1}{K_1} + \frac{(T_2 - T_1)}{K_2} + \frac{(T_f - T_2)}{K_2} & \tau_f \geq T_2 \end{cases}$$
(2.11)

where K_1 , K_2 , K_3 , T_1 , and T_2 are given by the manufacturer. When torsion of the harmonic drive is assumed to be caused by flexspline only, the torsion angle is defined as

$$\Delta \theta = \theta_{fo} - \theta_{fi} \tag{2.12}$$

where θ_{fo} denotes the flexible spline position at the load side.

In general, only the wave generator input position (motor's angle) and flexible output position (joint's angle) are measurable. These available position measurements can be used to calculate the harmonic drive torsion using the following relation

$$\Delta \theta = \theta_{fo} + \frac{\theta_w}{N}.$$
(2.13)

There is a need for a more comprehensive harmonic drive model that can capture all the harmonic drive behaviors including nonlinear compliance and hysteresis. In the previous work, this comprehensive model has been attempted by modeling each of these behaviors separately and then adding the resulted models to the basic model of equations Eq.(2.7) to Eq.(2.9). Such an approach led to complicated models with parameters that are hard to estimate. In addition, the proposed models where hysteresis was not neglected require the derivative of the torsion angle. This motivated our research objective of deriving a simple model that can capture the previously mentioned harmonic drive behavior without explicitly modeling them and does not require the noisy derivative of the torsion angle. Harmonic drive suffers not only nonlinear compliance but also hysteresis. In this section, we will investigate a two-spring system shown in Fig. 2.4 first.



Figure 2.4: A system of two springs and one mass: K_a and K_b represent the spring constant of (a) and (b), respectively.

In this system, the total displacement can be modeled as

$$X = \frac{F_a}{K_a} + \frac{F_b}{K_b}.$$
(2.14)

When F increases from 0, spring (a) is compressed and spring (b) stays at its initial position as long as $F < F_{fr}$. When $F > F_{fr}$, spring (b) is compressed by $(F - F_{fr})$. We can model the spring (b) force as Eq.(2.15) and displacement as Eq.(2.16).

$$F_a = F$$

$$F_b = F - F_{fr} sgn(\dot{F})$$
(2.15)

$$X = \frac{F}{K_a} + \frac{F}{K_b} - sgn(\dot{F})\frac{F_{fr}}{K_b}$$
(2.16)

where sign function is defined as

$$sgn(x) = \begin{cases} 1 & for \ x > 0, \\ 0 & for \ x = 0, \\ -1 & for \ x < 0. \end{cases}$$
(2.17)

Fig. 2.5 shows the force of spring (b), F_b , versus force applied to spring (a), F_a ; and Fig. 2.6 shows the stiffness curve and hysteresis caused by friction.


Figure 2.5: Spring (b) force versus force applied to spring (a).



Figure 2.6: Stiffness curve and the hysteresis caused by friction.

From above, we can conclude that there exists hysteresis between the external force F and the displacement X in the two spring system with friction. A simple rate-dependent hysteresis model as shown in Eq.(2.15) can capture this kind of hysteresis. However, the rate measurement is noisy and not reliable. On the other hand, when another external force is added to the other side of the two spring system as shown in Fig. 2.7, then F_b becomes an independent variable. In this case, there is no hysteresis relationship between F_a and F_b , and the rate-dependent hysteresis model does not work any more. However, Eq.(2.14) still works. If F_a and F_b can be measured, we can capture the system displacement X without considering hysteresis. And harmonic drive system is very similar to above two springs system with two external forces, it has external torque and wave generator torque. In most case, the external toque and the wave generator torque are independent.



Figure 2.7: A system of two springs and one mass with two external forces

To adequately describe the behavior of harmonic drive, the deformations of both the flexspline and the wave generator must be considered. An advantage of modeling the deformations of both is the capability of the model in capturing hysteresis behavior of the harmonic drive. It will be shown that a high fidelity harmonic drive model being able to capture complicated behaviors is achieved by modeling the compliance of the wave generator in addition to the compliance of the flexspline. When the wave generator's rigid elliptical inner-race is rotated, the flexspline molds into the rotating elliptical shape but does not rotate with it. The axes of these two elliptical shapes (WG and FS) are not always aligned, as shown in Fig. 2.8.

The reason behind this misalignment is the compliance of the wave generator, namely, the outer rim of the ball bearing. This misalignment depends on magnitude of the torque applied to the wave generator plug as well as the load torque. This compliance of the wave generator needs to be taking into account when modeling the harmonic drive compliance. In this section, a model of the compliance of flexspline and wave generator is derived first, then, the complete compliance model is given. Fig. 2.9 shows the diagram of harmonic drive considering flexspline and



Figure 2.8: Wave generator axes displacement



Figure 2.9: The kinematic representation of a harmonic drive showing flexspline and wave generator compliance

wave generator deformation.

Let us define the flexspline and wave generator torsion as

$$\Delta \theta_f = \theta_{fo} - \theta_{fi}, \tag{2.18}$$

$$\Delta \theta_w = \theta_{wo} - \theta_{wi}. \tag{2.19}$$

Comparing Fig. 2.9 with Fig. 2.2, from harmonic drive basic model Eq.(2.4), we have

$$\theta_{wo} = -N\theta_{fi}.\tag{2.20}$$

Eq.(2.20) can not be implemented as θ_{fi} may not be measured. However, the wave generator input position and the flexible output position are measured and can be used to calculate the harmonic drive torsion as given below

$$\Delta \theta = \theta_{fo} + \frac{\theta_{wi}}{N}.$$
(2.21)

By adding and subtracting the terms θ_{fi} and $\frac{\theta_{wo}}{N}$ from Eq.(2.21), we obtain

$$\Delta \theta = \theta_{fo} - \theta_{fi} + \left(\theta_{fi} + \frac{\theta_{wo}}{N}\right) - \left(\frac{\theta_{wo}}{N} - \frac{\theta_{wi}}{N}\right).$$
(2.22)

Substituting Eq.(2.18), Eq.(2.19) and Eq.(2.19) into Eq.(2.22), we obtain

$$\Delta \theta = \Delta \theta_f - \frac{\Delta \theta_w}{N}.$$
(2.23)

Eq.(2.10) and Eq.(2.11) give the nonlinear compliance of the flexspline, but they are not convenient to use. It is more suitable to describe the torsion angle as a function of the torque, especially for control purposes. By observing equation Eq.(2.10) and the stiffness curve in Fig. 2.10, it is clear that the local elastic coefficient increases with the increase of τ_f . If we define

$$K_{fl} = \frac{d\tau_f}{d\triangle\theta_f},$$

 K_{fl} should be a function of τ_f . Considering symmetric and using Taylor expansion, the local

elastic coefficient can be approximated by

$$K_{fl} = K_{f0} \left(1 + (c_f \tau_f)^2 \right), \qquad (2.24)$$

where, K_{f0} and c_f are constants to be determined.

Then, the torsion can be calculated as

$$\Delta \theta_f = \int_0^{\tau_f} \frac{d\tau_f}{K_{fl}}.$$
(2.25)

Substituting K_{fl} Eq.(2.24) into Eq.(2.25), we obtain

$$\Delta \theta_f = \frac{atan(c_f \tau_f)}{c_f K_{f0}}.$$
(2.26)

Remark 2 By observing equation Eq.(2.26), it is clear that τ_f can be easily obtained from $\Delta \theta_f$ and vice versa.

Let us consider that the hysteresis is caused by the wave generator torsion. When the motor output torque is within harmonic drive's starting torque, the harmonic drive's output torque will not change, which causes hysteresis. From Fig. 2.10, it can be seen that the hysteresis decreases to zero sharply at torque T_0 , which means that both of the stiffness and the local elastic coefficient increase sharply. Therefore, we model the wave generator local elastic coefficient as

$$K_{wl} = K_{w0} e^{c_w |\tau_w|},$$
(2.27)

where,

$$K_{wl} = \frac{d\tau_w}{d\triangle\theta_w}$$

 K_{w0} and c_w are constants to be determined.

The wave generator torsion angle can be calculated using the following relationship:

$$\Delta \theta_w = \int_0^{\tau_w} \frac{d_{\tau_w}}{K_{wl}}.$$
(2.28)

Substituting Eq.(2.27) into Eq.(2.28), we obtain

$$\Delta \theta_w = \frac{sgn\left(\tau_w\right)}{c_w K_{w0}} \left(1 - e^{-c_w |\tau_w|}\right). \tag{2.29}$$

Finally, the total deformation of the harmonic drive is approximated by synergetic integration of the flexspline and wave generator deformation that are given in Eq.(2.26) and Eq.(2.29), respectively.

Substituting them into Eq.(2.23), we obtain

$$\Delta \theta = \frac{a tan(c_f \tau_f)}{c_f K_{f0}} - \frac{sgn(\tau_w)}{c_w N K_{w0}} (1 - e^{-c_w |\tau_w|}).$$
(2.30)

2.3 Parameter Estimation

In this section, a systematic way of estimating the parameters of the proposed harmonic drive model is described. A typical stiffness and hysteresis curve of a harmonic drive, as provided by manufacture's specification sheet, is depicted in Fig. 2.10.

From the lower graph stiffness and hysteresis curve Fig. 2.10, assuming proposed model have same local elastic coefficient as piecewise model at center of piece, the local elastic coefficient at torque $T_1/2$ and $T_1/2 + T_2/2$ is K_1 and K_2 , respectively. These local elastic coefficients, K_1 and K_2 can be calculated using Eq.(2.24), as follows

$$K_1 = K_{f0} \left(1 + (c_f T_1/2)^2 \right), \qquad (2.31)$$

$$K_2 = K_{f0} \left(1 + (c_f (T_1 + T_2)/2)^2 \right).$$
(2.32)

By solving Eq.(2.31) and Eq.(2.32) for K_{f0} and c_f , we obtain

$$K_{f0} = K_1 + \frac{(K_1 - K_2)T_1^2}{(T_1 + T_2)^2 - T_1^2}$$
(2.33)

$$c_f = 2\sqrt{\frac{K_2 - K_1}{K_1(T_1 + T_2)^2 - K_2 T_1^2}}.$$
(2.34)



Figure 2.10: Typical stiffness and hysteresis curve of a harmonic drive.

For the wave generator, when the motor output torque is within harmonic drive's starting torque, the harmonic drive's output torque will not change, which causes hysteresis. Therefore, the stiffness of WG around zero output torque can be estimated using the following relationship:

$$K_{w0} = \frac{2\tau_{fs}}{N\Psi},\tag{2.35}$$

where, Ψ denotes the hysteresis loss and τ_{fs} is the harmonic drive's starting friction torque. From equation Eq.(2.29), we know the maximum torsion caused by the wave generator is $1/(c_w N K_{w0})$ at one direction. It is also evident from Fig. 2.10 that the total deformation caused by the wave generator at one direction is half of the hysteresis, Ψ . Therefore, we obtain

$$0.5\Psi = \frac{1}{c_w N K_{w0}}.$$
(2.36)

Solving Eq.(2.36), we have

$$c_w = \frac{2}{NK_{w0}\Psi}.$$
(2.37)

Simulations have been utilized to compare the performance of the proposed stiffness model with the linear piecewise model and the cubic polynomial model. Fig. 2.11 shows the simulation results for the piecewise linear model, the cubic polynomial model, and the proposed model, respectively. The results indicate that the proposed model matches others.



Figure 2.11: Simulation results of local elastic coefficient.



Figure 2.12: The stiffness curves for piecewise linear model, cubic polynomial model, and proposed model

2.4 Experimental Results

To monitor the behavior of the harmonic drive, a test station is set up as shown in Fig. 2.13, Fig. 2.14 and Fig. 2.15. The experimental diagram is as shown in Fig. 2.16. The harmonic drive is driven by a DC motor with a fixed output shaft position (with output rotationally locked). In this experiment, a brushed DC motor from Maxon, model 218014, is used. Its weight is 480g, with maximum rated torque of 18.8 *Ncm*, and torque constant of 0.321 *Nm/amp*. A linear power amplifier and the Q8 data acquisition board from Quanser Inc. are used to drive the motor and collect experimental data. The harmonic drive in the setup is SHD-17-100-2SH with gear ratio of 100:1, and rated torque of 16 *Nm* from Harmonic Drive AG.

Robotic joints are usually equipped with optical incremental encoder to measure the motorside position for control purposes as shown in Fig. 2.13. However, incremental encoders only provide the relative position of the motor shaft. Therefore, a method of determining the absolute position of the motor shaft is necessary. To obtain the motor absolute position, the joint is rotated 360° clockwise free-run while recording the flexspline output position at each encountered index of the incremental encoder, $\theta_{fo}^{cw_i}$. Then the joint is rotated 360° counterclockwise, and the flexspline output position (the link-side absolute encoder readings) at each index $\theta_{fo}^{ccw_i}$ is recorded. For one complete rotation, there are N indexes. The offset of the incremental



Figure 2.13: Schematic diagram of experimental setup.



Figure 2.14: Cross-sectional view of the experimental joint



Figure 2.15: A picture of the experimental setup

encoder installed at the motor side is determined as

$$\theta_{offset} = \sum_{i=0}^{N-1} \frac{(\theta_{fo}^{cw_i} + \theta_{fo}^{ccw_i} - 2i360/N)}{2N},$$
(2.38)

where θ_{offset} is the offset between the link-side absolute position measurement and the motorside incremental encoder relative position measurement, N is the gear ratio which equals to the number of indexes.

The absolute position of the motor shaft is estimated using the recorded link-side positions, θ_{fo0} , at the first encountered index after power-on, as

$$\theta_{wi} = \theta_{offset} + \frac{360}{N} \operatorname{int}(\frac{N}{360}(\theta_{fo0} - \theta_{offset}) + 0.5) + \theta_{IE}, \qquad (2.39)$$

where θ_{IE} is the incremental encoder reading, and int(.) is a conversion function that converts float to integer data type. This algorithm will be implemented in the "SSi to USB and Relative to Absolute" block of diagram shown in Fig. 2.16.



Figure 2.16: Schematic diagram of experiment.

Two experiments were conducted. In the first experiment, a controlled torque was applied to the wave generator with a fixed output link (FS). In this case, the torsion across the harmonic drive was measured using two encoders, one on the motor-side and another on the link-side, the output torque was measured by link-side force sensor, and applied torque at wave generator was calculated from the command torque. In the second experiment, a position controller was used to hold the wave generator at a fixed position (with input rotationally locked), and both forward as well as backward torque was applied to the link. In this case, torsion across the harmonic drive was measured by two encoders, the link-side torque was measured by link-side force sensor, and the wave generator torque was calculated using static friction model.

From manufacture's catalogue (Harmonic Drive LLC 2012), the following parameters were obtained:

$$K_1 = 8.4 \times 10^3 \ Nm/rad,$$

 $K_2 = 9.4 \times 10^3 \ Nm/rad,$
 $T_1 = 3.9 \ Nm,$
 $T_2 = 12 \ Nm.$

 K_{f0} and c_f can be obtained by solving equations Eq.(2.33) and Eq.(2.34) as given below

$$K_{f0} = 8.2 \times 10^3 \ Nm/rad,$$

 $c_f = 0.012 \ Nm^{-1}.$

Also from manufacture's datasheet, one can obtain Ψ , i.e., $\Psi = 2.9 \times 10^{-4}$ rad. Two quantities are measured, the starting torque on wavegenerator τ_{fs} and back-driving torque on flexspline τ_{fb} .

$$\tau_{fs} = 1.2Ncm,$$

$$\tau_{fb} = 2.0 Nm.$$

Using the above constants and substituting into Eq.(2.35), the K_{w0} can be calculated as shown below

$$K_{w0} = \frac{2 \times 1.2 \times 10^{-2}}{100 \times 2.9 \times 10^{-4}} = 0.83 \ Nm/rad.$$

By plugging K_{w0} and Ψ in equation Eq.(2.36), one can obtain

$$c_w = \frac{2}{100 \times 0.83 \times 2.9 \times 10^{-4}} = 83.1 \ Nm^{-1}.$$

These parameters are calculated to be used with the harmonic drive model of equation Eq.(2.30). Once the model parameters are calculated and/or estimated, the model can be tested by comparing its performance to the experimental data.



Figure 2.17: Motor-side input torque signal history

In the first experiment, to observe the harmonic drive stiffness and hysteretic behavior, a sinusoid torque command signal with monotonically decreasing amplitude is used to drive the DC motor as depicted in Fig. 2.17.

The torsion across the harmonic drive is measured by simultaneously reading the encoders mounted on the output-side (flexspline) as well as the motor-side. The empirical data collected from the first experiment along with the model based torsion versus the input torque values are depicted in Fig. 2.18. The estimation error of the classic model given in Eq.(2.11) and that of the proposed model in Eq.(2.30) are shown in Fig. 2.19, Fig. 2.20. The results show that the proposed model can achieve better torsion estimation. This is due to the fact that the proposed model captures the hysteresis behavior of the harmonic drive. As shown in Fig. 2.20, the estimation errors form two similar curves. The pattern of the two similar curves is related to the kinematic error, while the distance between the two curves represents hysteresis error. The proposed model reduces the distance between the two curves, that is, reduces the hysteresis error. Based on this experiment, the estimation error was reduced from $\pm 2.3 \times 10^{-4}$ rad to $\pm 1.7 \times 10^{-4}$ rad. The remaining error is caused by the unmodeled kinematic error. The simple and efficient compliance model proposed in this work achieves estimation errors similar to those achieved by the more complicated models, e.g., the work presented by (Preissner et al. 2012).

In the second experiment, a bidirectional external torque is applied on flexspline side as shown in Fig. 2.21. The motor-side torque (wave generator torque) is estimated using the following



Figure 2.18: Motor-side input torque versus output torsion



Figure 2.19: Comparison of estimation error versus time



Figure 2.20: Comparison of estimation error versus motor positions

equations where the measured back-driving friction torque, τ_{fb} , was used:

If
$$(\tau_f(t) + N\tau_w(t-1) > \tau_{fb}), \quad \tau_w(t) = -(\tau_f(t) - \tau_{fb})/N$$

if $(\tau_f(t) - N\tau_w(t-1) > -\tau_{fb}), \quad \tau_w(t) = -(\tau_f(t) + \tau_{fb})/N$ (2.40)
else, $\tau_w(t) = \tau_w(t-1).$

The harmonic drive torsional angle is obtained by substituting the measured link-side position and the motor-side position into Eq.(2.21). Comparison between the measured torsional angle the torsion estimated using Eq.(2.30) is shown in Fig. 2.22. The agreement between the predicted torsional compliance and the experimental data in both experiments confirmed the validity of the proposed model.



Figure 2.21: External torque applied on the output-side



Figure 2.22: Output torque versus output torsion

2.5 Conclusion

A novel mathematical model for the compliance of harmonic drives has been presented. When combined with a simple friction model, the proposed model captures the nonlinear stiffness and hysteresis phenomenon of harmonic drive transmission. Numerical simulations and experiments have been used to test the proposed modeling concept; accurate match in the result confirmed the reliability of the proposed model. Advantages of the model include its simple structure, its ability of capturing hysteresis, and the method of verification. The proposed modeling approach does not require detailed knowledge of the gear tooth geometry or wave generator kinematics to account for hysteresis model as in other proposed works. The model was compared with measurements for two cases, one in which the output shaft is rotationally locked and the other one when the shaft is free to rotate. The proposed model resolve the difficulties in estimating harmonic drive model parameters associated with many of the previously proposed models and can predict the harmonic drive behavior at operating points different than those used for model identification.

Chapter 3

Torque Estimation with Harmonic Drive Compliance Model

3.1 Torque Estimation

In the last chapter, we considered harmonic drive flexspline and wave generator bearing deformation. The harmonic drive output angle usually differs from the theoretical angle even with consideration of flexibility. The kinematic position error is the difference between the theoretical and actual output rotation angles at zero torque. The literature, however, still lacks a precise characterization of the mechanism responsible for the kinematic error. First, the origin of kinematic-error is not known precisely. Nye and Kraml (1991) had demonstrated that typical kinematical-error signatures vary periodically at one and two times the rotational frequency of the wave generator and subsequent harmonics. Tuttle and Seering (1993) carried out a mathematical analysis regarding the source of kinematic error and concluded that the error is due to assembly and physical imperfections on the three principal elements of a harmonic drive.

In this section, we try to estimate the transmitted torque using harmonic drive deformation. The kinematic error will affect the estimation. Assuming the transmitted torque is around harmonic drive rated torque, the local stiffness will be around K_2 , and the related torque estimation error will be

$$\tau_{kerr} = K_2 \theta_{err}. \tag{3.1}$$

Table 3.1: Theoretical torque estimation error caused by kinematic error for SHD series Harmonic Drive

Size	Ratio	Rated torque	K_2	Max Kinematic	Max Torque	Relative
		(Nm)	$10^4 \left(Nm/Rad \right)$	error $10^{-4} (Rad)$	error (Nm)	error (%)
14	50	3.7	0.37	4.4	1.6	43
14	100	5.4	0.44	4.4	1.9	35
17	50	11.0	0.88	4.4	3.8	35
	100	16.0	0.94	4.4	4.1	25
20	50	17	1.3	2.9	3.7	21
	100	28	1.7	2.9	4.9	17
	160	28	1.7	2.9	4.9	17
25	50	27	2.7	2.9	7.8	29
	100	47	3.7	2.9	10.7	23
	160	47	3.7	2.9	10.7	23
32	50	53	6.1	2.9	17.7	33
	100	96	7.8	2.9	22.6	24
	160	96	7.8	2.9	22.6	24
	50	96	11.0	2.9	31	32
40	100	185	14.0	2.9	40	22
	160	206	14.0	2.9	40	19

Define the relative torque estimation error as

$$relative \, error = \frac{\tau_{kerr}}{rated \, torque} \times 100\%, \tag{3.2}$$

Table. 3.1 (Harmonic Drive LLC 2012) gives the position accuracy (maximum kinematic error) of all SHD series harmonic drives, as well as the absolute and relative torque estimation accuracy related to position accuracy. From the table, we can see that the torque estimation accuracy will be very low if we don't consider kinematic errors.

To achieve a relative accurate torque estimation, the kinematic error must be included. The kinematic error can be measured for one complete output revolution using the high resolution link side absolute encoder. The dashed blue curve in Fig. 3.1 shows the kinematic error distribution based on the link side position.



Figure 3.1: Kinematic error distribution based on link position

By using Fourier curve fitting, we can model the kinematic error as following

$$\theta_{errl} = a_{l0} + a_{l1}\cos(\theta_{fo}w_l) + b_{l1}\sin(\theta_{fo}w_l), \tag{3.3}$$

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the result is shown as a red solid curve in Fig. 3.1. If we define

$$\theta_{errw} = \theta_{err} - \theta_{errl}, \tag{3.4}$$

and map θ_{errw} to motor side position, we can get the residual distribution as dashed blue in Fig. 3.2. Also by using Fourier curve fitting, we can model the residual kinematic error as



Figure 3.2: Kinematic error distribution based on motor position

$$\theta_{errw} = a_{w0} + a_{w1}\cos(\theta_{wi}w_w) + b_{w1}\sin(\theta_{wo}w_w) + a_{w2}\cos(2\theta_{wi}w_w) + b_{w2}\sin(2\theta_{wi}w_w).$$
(3.5)

The modeled residual part is shown as a red solid curve in same figure. So the total kinematic error can be modeled as Eq.(3.6)

$$\theta_{err} = \theta_{errl} + \theta_{errw}, \tag{3.6}$$

$$\theta_{err} = a_0 + a_{l1}cos(\theta_{fo}w_l) + b_{l1}sin(\theta_{fo}w_l) + a_{w1}cos(\theta_{wi}w_w) + b_{w1}sin(\theta_{wo}w_w) + a_{w2}cos(2\theta_{wi}w_w) + b_{w2}sin(2\theta_{wi}w_w),$$
(3.7)

where $a_0, a_{l1}, b_{l1}, w_l, a_{w1}, a_{w2}, b_{w1}, b_{w2}, w_w$ are parameters determined as in Table. 3.2.

parameters	Value
a_0	0
a_{l1}	-0.0001476
b_{l1}	-0.004309
w_l	0.01731
a_{w1}	0.001594
b_{w1}	-0.001891
a_{w2}	0.003288
b_{w2}	0.0009049
w_w	0.01734

Table 3.2: Kinematic error modeling parameters

The total modeled kinematic error is shown in Fig. 3.3.



Figure 3.3: Modeled kinematic error.

Considering kinematic error, Eq.(2.23) can be modified as

$$\Delta \theta = \Delta \theta_f - \frac{\Delta \theta_w}{N} + \theta_{err}.$$
(3.8)

So after we get the kinematic error, the torque can be estimated by Eq.(3.9).

$$\Delta \theta_f = \Delta \theta + \frac{sgn\left(\tau_w\right)}{c_w N K_{w0}} \left(1 - e^{-c_w |\tau_w|}\right) - \theta_{err}$$
(3.9)

The total torsional deformation of the harmonic drive is measured using both link-side and motor-side encoders. The wave generator torque τ_w is approximated by the motor torque command. The flexspline torsional deformation cab be calculated by Eq.(3.9).

Having the flexspline torsional deformation, $\triangle \theta_f$, the joint torque estimate is obtained using the inverse of Eq.(2.26).

$$\tau_f = \frac{\tan(\triangle \theta_f c_f K_{f0})}{c_f} \tag{3.10}$$

A block diagram illustrating the proposed torque estimation method is portrayed in Fig. 3.4.



Figure 3.4: Block diagram of the proposed torque estimation technique

3.2 Experimental Setup and Results

To verify the proposed torque estimation method, we have conducted three sets of experiments. The test station was set up as shown in Fig. 2.13, Fig. 2.14, Fig. 2.15 and Fig. 3.5. The base joint (joint 1) in Fig. 2.15 is developed in our laboratory to investigate the performance of the proposed joint torque estimation method. In these experimental setups, the harmonic drive of

joint 1 is driven by a brushed DC motor from Maxon, model 218014. A linear power amplifier and the Q8 data acquisition board from Quanser Inc. are used to drive the motor and collect experimental data. The harmonic drive in the setup is SHD-17-100-2SH with gear ratio of 100:1, and rated torque of 16 Nm from Harmonic Drive AG. The link position sensor is able to measure the off-drive position with an accuracy of better than 0.01 degree. As the absolute position is measured no reference sequences have to be performed during the power up of the robot. The sensor has a flat shape and allows the use of a huge hallow shaft. The link-side torque is measured using an ATI six-axis force/torque sensor, Mini45-ERA. A cross-sectional view of the developed robotic joint with the link-side encoder is shown Fig. 2.14.



Figure 3.5: Picture of experiment setup: (a)without payload; (b)with payload

In first experiment, the setup is shown as in Fig. 2.15. The joint is open-loop controlled in torque mode at different torque outputs. The efficiency of the proposed torque estimation method is verified by comparing the estimated joint torque with a torque measurement from the ATI force/torque sensor mounted on the output of the base joint. The external torque is added manually as a disturbance, and the results are depicted in Fig. 3.9 and Table. 3.3. In the second experiment setup, Joint 2, joint 3, and the link are used as payload as shown

Motor Output Torque (Ncm)	0	3	-3	5	-5	10	-10
Maxspeed(Rad/s)	0.02	1.43	-1.30	1.50	-1.41	1.56	-1.56
Max Torque Error (Nm)	0.3	0.2	0.6	0.8	0.7	1.0	0.6
MinTorqueError(Nm)	-0.5	-1.2	-1.1	-1.2	-1.3	-0.9	-2.3

Table 3.3: Torque estimation error at different motor outputs

in Fig. 3.5(a). The accuracy of the proposed torque estimation method is verified by comparing the estimated joint torque with the torque measurement from the ATI force/torque sensor mounted on the output of the base joint. Both slow and sudden changes of the load were applied and the results are depicted in Fig. 3.6 and Fig. 3.7. Slow changes of the load torque were introduced by controlling the joint motion with a sinusoidal desired trajectory. The moving links and the joints attached to the base joint introduce a gradually changing load torque. To introduce sudden changes to the load torque, an external torque was applied manually in both directions. The error in torque estimation is around 1Nm, which is comparable with the commercial F/T sensor. In the last experiment setup, an additional payload is added at 400mm



Figure 3.6: Estimated torque versus torque measured by F/T sensor (response to slow changes)

horizontal distance from center of joint 1 as shown in Fig. 3.5(b). The payload is suddenly removed by cutting the wire. The result is shown in Fig. 3.8. The result shows the proposed estimation has a relatively good dynamic response.



Figure 3.7: Estimated torque versus torque measured by F/T sensor (response to fast changes)



Figure 3.8: Torque estimation at payload suddenly change









Figure 3.9: Snapshots for torque estimation at different motor output

Chapter 4

Multiple Mode Control of MRR with HDT Joint

In this chapter, a multiple mode control method using the estimated torque is developed for the MRR robotic joint, making it work in active mode with position control, or passive mode with friction compensation. A robust adaptive control algorithm is developed for motion control of MRR in active mode; and an friction compensation technique is proposed to make it capable of working in passive mode.

4.1 MRR Joint Dynamics

Considering an MRR constructed with n actuator modules and n links, each module is integrated with a rotary joint with a harmonic drive and two encoders as illustrated in Fig. 4.1. Similarly as in (Imura et al. 1991), we assume:

Assumption 1 The rotor is symmetric with respect to the axis of rotation.

Assumption 2 The torque transmission does not fail at the speed reducer.

Consider a modular and reconfigurable articulated robot with modules installed in series. Each module provides a rotary joint. The base module is named the first module. Modules close to the first module are denoted as lower modules, and modules close to the end-effector are called upper modules. For the *i*th module, we use the following notations:



Figure 4.1: Schematic diagram of an MRR module

 I_{mi} :moment of inertia of the *i*th rotor about the axis of rotation;

 I_{li} :moment of inertia of the *i*th link about the axis of rotation;

 N_i : reduction ratio of the speed reducer ($N_i \ge 1$);

 q_{mi} : motor position of the *i*th joint;

 q_{li} : link position of the *i*th joint;

 $f_{mi}(q_{mi}, \dot{q}_{mi})$: joint friction on motor side, assumed to be a function of motor position and velocity;

 $f_{li}(q_{li}, \dot{q}_{li})$: joint friction on link side, assumed to be a function of link position and velocity;

 $g_{li}(q_{l0}...q_{li})$: link gravity of the *i*th joint;

 τ_{exti} : External torque added to link of the *i*th joint;

 τ_{ti} : Torque transferred at transmission system of the *i*th joint;

 τ_{mi} : motor output torque of the *i*th joint;

 z_{mi} :unity vector along the axis of rotation of the *i*th joint;

 z_{li} :unity vector along the axis of rotation of the *i*th link;

The dynamic equations at motor side and link side for each module are formulated as follows: for the base module, i = 1

$$I_{l1}\ddot{q}_{l1} + f_{l1}(q_{l1}, \dot{q}_{l1}) + g_{l1}(q_{l1}) = \tau_{t1} + \tau_{ext1};$$
(4.1)

$$I_{m1}\ddot{q}_{m1} + f_{m1}(q_{m1}, \dot{q}_{m1}) + \frac{\tau_{t1}}{N_1} = \tau_{m1};$$
(4.2)

for the second module from the base, i=2

$$I_{l2}\ddot{q}_{l2} + f_{l2}(q_{l2}, \dot{q}_{l2}) + I_{l2}z_{l2}^T z_{l1}\ddot{q}_{l1} + g_{l2}(q_{l1}, q_{l2}) = \tau_{t2} + \tau_{ext2};$$
(4.3)

$$I_{m2}\ddot{q}_{m2} + f_{m2}(q_{m2}, \dot{q}_{m2}) + I_{m2}z_{m2}^T z_{l1}\ddot{q}_{l1} + \frac{\tau_{t2}}{N_2} = \tau_{m2};$$
(4.4)

for the upper joints, $i \ge 3$

$$I_{li}\ddot{q}_{li} + f_{li}(q_{li}, \dot{q}_{li}) + I_{li} \sum_{j=1}^{i-1} z_{li}^T z_{lj} \ddot{q}_{lj} + I_{li} \sum_{j=2}^{i-1} \sum_{k=1}^{j-1} z_{li}^T \left(z_{lk} \times z_{lj} \right) \dot{q}_{lk} \dot{q}_{lj} + g_{li}(q_{l1}, \dots, q_{li}) = \tau_{ti} + \tau_{exti};$$

$$(4.5)$$

$$I_{mi}\ddot{q}_{mi} + f_{mi}(q_{mi}, \dot{q}_{mi}) + I_{mi}\sum_{j=1}^{i-1} z_{mi}^T z_{lj}\ddot{q}_{lj} + I_{mi}\sum_{j=2}^{i-1}\sum_{k=1}^{j-1} z_{mi}^T \left(z_{lk} \times z_{lj}\right)\dot{q}_{lk}\dot{q}_{lj} + \frac{\tau_{ti}}{N_i} = \tau_{mi}.$$
 (4.6)

The link side friction $f_{li}(q_{li}, \dot{q}_{li})$ is assumed to be a function of the link position and velocity (Liu 2002; Armstrong-Helouvry et al. 1994).

$$f_{li}(q_{li}, \dot{q}_{li}) = (f_{lci} + f_{lsi} \exp(-f_{l\tau i} \dot{q}_{li}^2)) sgn(\dot{q}_{li}) + b_{li} \dot{q}_{li} + f_{qli}(q_{li}, \dot{q}_{li})$$
(4.7)

Similarly, the rotor side friction can be modeled as

$$f_{mi}(q_{mi}, \dot{q}_{mi}) = (f_{mci} + f_{msi} \exp(-f_{m\tau i} \dot{q}_{mi}^2)) sgn(\dot{q}_{mi}) + b_{mi} \dot{q}_{mi} + f_{qmi}(q_{mi}, \dot{q}_{mi}), \quad (4.8)$$

where f_{lci} and f_{mci} denote the Coulomb friction-related parameters on link side and motor side, respectively; f_{lsi} and f_{msi} represent the static friction friction-related parameters; $f_{l\tau i}$ and $f_{m\tau i}$ are the positive parameters corresponding to the Stribeck effect; b_{li} and b_{mi} denote the viscous friction coefficients; f_{qli} and f_{qmi} reflect the position dependency of friction and other friction modeling errors. The sign function is defined as Eq.(2.17).

The dynamic model is formulated to include Coulomb friction, static friction, Stribeck effect, position dependency, and other bounded disturbances. In this model, we neglect frictional memory and rising static friction as discussed by Armstrong et al. (1994).

4.2 Robust Adaptive Control in Active Mode with the Estimated Torque

Easily changing configurations to deal with different tasks is the advantage of the modular and reconfigurable robot, but with the reconfiguration, the robot dynamic parameters also change. Therefore, controllers designed based on one configuration dynamics will not work well when the MRR is reconfigured. This is the reason why the decentralized control technique is applied in our research. For the decentralized control, each joint is considered as an independent subsystem, and the dynamic effects from the other links and joints are treated as disturbances. Therefore, the decentralized control is suitable for independent robot configurations so as to achieve modularity in software.

Because of the decentralized control, the controller doesn't know where the module is installed, and what the link parameters are. When we review the dynamic equations Eq.(4.4) and Eq.(4.5). we don't know any parameter in Eq.(4.4). But it is possible to consider the dynamics equations at the motor side and the link side separately in a joint with a torque sensor (Kawakami et al. 2010). The moment of inertia of the *i*th rotor about its axis of rotation, I_{mi} , is a physical parameter of the *i*th module, which can be identified offline and does not change with the robot reconfiguration. The joint friction at the rotor side is another major source of model uncertainty. The friction model parameters b_{mi} , f_{mci} , f_{msi} and $f_{m\tau i}$ are not accurately known, and not necessarily constant. However, their nominal values can be determined offline as constants. The nominal values of b_{mi} , f_{mci} , f_{msi} and $f_{m\tau i}$ are denoted as \hat{b}_{mi} , \hat{f}_{msi} and $\hat{f}_{m\tau i}$, respectively.

Model uncertainty in the third term of Eq.(4.6), $I_{mi} \sum_{j=1}^{i-1} z_{mi}^T z_{lj} \ddot{q}_{lj}$, can result from the robot reconfiguration, such as misalignment of the axes. The magnitude of this uncertainty is dependent upon the accelerations of the first i - 1 joints. Model uncertainty in the fourth term of Eq.(4.6), $I_{mi} \sum_{j=2}^{i-1} \sum_{k=1}^{j-1} z_{mi}^T (z_{lk} \times z_{lj}) \dot{q}_{lk} \dot{q}_{lj}$, can also result from the robot reconfiguration. The magnitude of this model uncertainty is dependent upon the velocities of all of the first i - 1 joints.

Let $F_{mi} = [b_{mi} f_{mci} f_{msi} f_{m\tau i}]^T$. According to the model uncertainty decomposition scheme proposed in (Liu et al. 2006), F_{mi} can be decomposed into a constant part plus a variable part,

i.e.,

$$F_{mi} = F_{mi}^c + F_{mi}^v, (4.9)$$

where the superscripts "c" and "v" represent constant and variable part, respectively.

Property 1 *The variable part in Eq.(4.9) is bounded, i.e.,*

$$|F_{mi}^{v}| < \rho_{F_{mi}},$$
 (4.10)

where $\rho_{F_{mi}}$ is the constant bound.

Assumption 3 The nonparametric friction term in Eq.(4.8) is bounded, i.e.,

$$\left|f_{qmi}\left(q_{mi}, \dot{q}_{mi}\right)\right| < \rho_{fqmi},\tag{4.11}$$

where $\rho_{f_{ami}}$ is a known constant bound for any positions q_{mi} and velocities \dot{q}_{mi} .

Assumption 4 Since z_{mi} , z_{lj} and z_{lk} are unit vectors, the resulting vector products $z_{mi}^T(z_{lk} \times z_{lj})$ and $z_{mi}^T z_{lj}$ are bounded. Furthermore, as the base robotic arm is stabilized, the accelerations (\ddot{q}_{lj}) and velocities (\dot{q}_{lj} , \dot{q}_{lk}) of the robotic arm joints must be bounded. Hence, the inertial and Coriolis forces associated with motion of the base robotic arm are bounded, i.e., if we define

$$\rho_{\alpha_{base}} > max \left| \sum_{j=1}^{i-1} z_{mi}^T z_{lj} \ddot{q}_{lj} + \sum_{j=2}^{i-1} \sum_{k=1}^{j-1} z_{mi}^T \left(z_{lk} \times z_{lj} \right) \dot{q}_{lk} \dot{q}_{lj} \right|$$
(4.12)

for any possible configuration, then

$$|\tau_{basei}| = I_{mi} \left| \sum_{j=1}^{n} z_{mi}^{T} z_{lj} \ddot{q}_{lj} + \sum_{j=2}^{n} \sum_{k=1}^{j-1} z_{mi}^{T} \left(z_{lk} \times z_{lj} \right) \dot{q}_{lk} \dot{q}_{lj} \right| < I_{mi} \rho_{base}, \tag{4.13}$$

where ρ_{base} is a constant bound.

Assumption 5 The torque estimation inaccuracy and noise is bounded; furthermore, the estimate error of τ_{ti} is bounded i.e.,

$$|\tilde{\tau}_{ti}| = |\tau_{ti} - \hat{\tau}_{ti}| < \rho_{\tau_{ti}},$$
(4.14)

where $\hat{\tau}_{ti}$ is the torque estimation in the last chapter, $\rho_{\tau_{ti}}$ are known constant bounds.

Define the system errors as

$$e_{i} = q_{mi} - q_{mi}^{a},$$

$$r_{i} = \dot{e}_{i} + \lambda_{i}e_{i},$$

$$a_{i} = \ddot{q}_{mi}^{d} - 2\lambda_{i}\dot{e}_{i} - \lambda_{i}^{2}e_{i},$$

$$(4.15)$$

where q_{mi}^d is the desired joint space motion for the i_{th} joint, which may be derived from the desired link side with the inverse dynamics; \dot{q}_{mi}^d denotes the corresponding joint-space motor side velocity; \ddot{q}_{mi}^d represents the desired joint-space motor side accelerations; λ_i is a positive constant.

Let \hat{b}_{mi}^c , \hat{f}_{mci}^c , \hat{f}_{msi}^c and $\hat{f}_{m\tau i}^c$ represent estimations of the constant friction parameters and using the linearization scheme proposed in (Liu et al. 2006), the friction model shown in Eq.(4.8) can be approximated by

$$f_{mi}(q_{mi}, \dot{q}_{mi}) \approx \hat{f}_{mi}^{c}(\dot{q}_{mi}) + Y_{i}(\dot{q}_{mi})\left(\tilde{F}_{mi}^{c} + F_{mi}^{v}\right) + f_{qmi}(q_{mi}, \dot{q}_{mi}) + \check{f}_{mi}(\dot{q}_{mi}), \quad (4.16)$$

where $\tilde{F}_{mi}^c = F_{mi}^c - \hat{F}_{mi}^c$ with $\hat{F}_{mi}^c = [\hat{b}_{mi}^c \ \hat{f}_{mci}^c \ \hat{f}_{msi}^c \ \hat{f}_{m\tau i}^c]^T$; $\hat{f}_{mi}^c \ (\dot{q}_{mi})$, $\check{f}_{mi} \ (\dot{q}_{mi})$, and $Y_i \ (\dot{q}_{mi})$ can be detailed as follows:

$$\hat{f}_{mi}^{c}(\dot{q}_{mi}) = \left[\hat{f}_{mci}^{c} + \hat{f}_{msi}^{c}\exp\left(-\hat{f}_{m\tau i}^{c}\dot{q}_{mi}^{2}\right)\right]sat(\dot{q}_{mi},\epsilon_{\dot{q}_{mi}}) + \hat{b}_{mi}^{c}\dot{q}_{mi},
\tilde{f}_{mi}(\dot{q}_{mi}) = \left[f_{mci} + f_{msi}\exp\left(-f_{m\tau i}\dot{q}_{mi}^{2}\right)\right]\left[sgn(\dot{q}_{mi}) - sat(\dot{q}_{mi},\epsilon_{\dot{q}_{mi}})\right]
Y_{i}(\dot{q}_{mi}) = \left[0\ 1\ \exp(-\hat{f}_{m\tau i}^{c}\dot{q}_{mi}^{2}) - \hat{f}_{msi}^{c}\dot{q}_{mi}^{2}\exp(-\hat{f}_{m\tau i}^{c}\dot{q}_{mi}^{2})\right]
\cdot sat(\dot{q}_{mi},\epsilon_{\dot{q}_{mi}}) + \left[\dot{q}_{mi}\ 0\ 0\ 0\right],$$
(4.17)

where $\epsilon_{\dot{q}_i}$ is a positive constant, sat(x,y) is the saturation function defined as follows:

$$sat(x,y) = \begin{cases} \frac{x}{|x|} & |x| > y\\ \frac{x}{|y|} & |x| \le y, \end{cases}$$
(4.18)

Assumption 6 The last item in Eq.(4.16) $\check{f}_{mi}(\dot{q}_{mi})$ is bounded, i.e., $|\check{f}_{mi}(\dot{q}_{mi})| < \rho_{f_{mi}}$.

To follow the desired trajectories in joint space, a robust adaptive control law is designed as

follows:

$$\tau_{mi} = I_{mi}a_{i} + \frac{\hat{\tau}_{ti}}{N_{i}} + \hat{f}_{mi}^{c}(\dot{q}_{mi}) - K_{Ii} \int_{0}^{t} r_{i}(t) dt - \left(\rho_{f_{mi}} + \rho_{f_{qmi}} + I_{mi}\rho_{base} + \frac{\rho_{\tau ti}}{N_{i}}\right) \cdot sat(r_{i}, \epsilon_{ri}) - \sum_{j=1}^{4} \left\{\rho_{F_{mij}}Y_{ij}(\dot{q}_{mi}) sat(r_{i}Y_{ij}(\dot{q}_{mi}), \epsilon_{F_{mij}})\right\},$$
(4.19)

where $Y_{ij}(\dot{q}_{mi})$ is the j_{th} element of $Y_i(\dot{q}_{mi})$, and ϵ_{ri} and $\epsilon_{F_{mij}}$ are positive control parameters,

Theorem 1 Given the module reconfigurable robot, the joint dynamics as given in Eq.(4.6), the tracking error of each joint is uniformly ultimately bounded under the control law given by Eq.(4.19) and the adaption law of $\dot{F}_{mi}^c = -\mu_{Fic} [Y_i(\dot{q}_i)]^T r_i$ with a positive constant μ_{Fic} .

proof 1 Consider the Lyapunov function candidate

$$V = \frac{1}{2}I_{mi}r_i^2 + \frac{1}{2}k_{Ii} \left[\int_0^t r_i(t) dt\right]^2 + \frac{1}{2} \frac{\left(\tilde{F}_{mi}^c\right)^T \tilde{F}_{mi}^c}{\mu_{Fic}},$$
(4.20)

Differentiating Eq.(4.20), it yields

$$\dot{V} = r_i \left\{ I_{mi} \dot{r}_i + k_{Ii} \int_0^t r_i(t) dt \right\} + \frac{\left(\dot{\tilde{F}}_{mi}^c\right)^T \tilde{F}_{mi}^c}{\mu_{Fic}}.$$
(4.21)

Substituting Eq.(4.15) and Eq.(4.19) into Eq.(4.6), we obtain

$$r_{i}\left\{I_{mi}\dot{r}_{i}+K_{Ii}\int_{0}^{t}r_{i}(t) dt\right\} = -I_{mi}\lambda_{i}r_{i}^{2}-r_{i}f_{mi}(q_{mi},\dot{q}_{mi})-r_{i}\tau_{basei} -r_{i}\left[\frac{\tilde{\tau}_{ti}+\rho_{\tau ti}sat(r_{i},\epsilon_{ri})}{N_{i}}\right]-r_{i}\left(\rho_{f_{mi}}+\rho_{f_{qmi}}+I_{mi}\rho_{base}\right)sat(r_{i},\epsilon_{ri}) -r_{i}\sum_{j=1}^{4}\left\{\rho_{F_{mij}}Y_{ij}(\dot{q}_{mi})\cdot sat\left(r_{i}Y_{ij}(\dot{q}_{mi}),\epsilon_{F_{mij}}\right)\right\}+r_{i}\hat{f}_{mi}^{c}(\dot{q}_{mi}).$$
(4.22)

Since F_{mi}^c is a constant vector, we have

$$\dot{\tilde{F}}_i^c = -\dot{\hat{F}}_i^c.$$

Substituting Eq.(4.22) and the adaption law into Eq.(4.21), and considering saturation function

Eq.(4.18), we can obtain

$$\dot{V} = -I_{mi}\lambda_{i}r_{i}^{2} - r_{i}\left[\check{f}_{mi}\left(\dot{q}_{mi}\right) + \rho_{f_{mi}}sat\left(r_{i},\epsilon_{ri}\right)\right] - \frac{r_{i}\left[\check{\tau}_{ti} + \rho_{\tau ti}sat(r_{i},\epsilon_{ri})\right]}{N_{i}} \\
-r_{i}\left[f_{q_{mi}}\left(q_{mi},\dot{q}_{mi}\right) + \rho_{f_{qmi}}sat\left(r_{i},\epsilon_{ri}\right)\right] - r_{i}\left[\tau_{basei} + I_{mi}\rho_{base}sat\left(r_{i},\epsilon_{ri}\right)\right] \\
-\sum_{j=1}^{4}\left\{r_{i}Y_{ij}\left(\dot{q}_{mi}\right)\left[F_{ij}^{v} + \rho_{F_{mij}}sat\left(r_{i}Y_{ij}\left(\dot{q}_{i}\right),\epsilon_{F_{mij}}\right)\right]\right\},$$
(4.23)

where F_{mij}^{v} and $\rho_{F_{mij}}$ are the j_{th} element of F_{mi}^{v} and $\rho_{F_{mi}}$, respectively.

From Assumptions 3–6, if $|r_i| > \epsilon_{ri}$, the second to fifth items in Eq.(4.23) are negative, i.e.,

$$-r_{i}\left[\check{f}_{mi}\left(\dot{q}_{mi}\right) + \rho_{fi} \cdot sat\left(r_{i}, \epsilon_{ri}\right)\right] < 0,$$

$$-\frac{1}{N_{i}} \cdot r_{i}\left[\tilde{\tau}_{ti} + \rho_{\tau ti} \cdot sat\left(r_{i}, \epsilon_{ri}\right)\right] < 0,$$

$$-r_{i}\left[f_{qmi}\left(q_{mi}, \dot{q}_{mi}\right) + \rho_{f_{qmi}} \cdot sat\left(r_{i}, \epsilon_{ri}\right)\right] < 0,$$

$$-r_{i}\left[\tau_{basei} + I_{mi}\rho_{\alpha_{base}} \cdot sat\left(r_{i}, \epsilon_{ri}\right)\right] < 0.$$
(4.24)

If $|r_i| \leq \epsilon_{ri}$, we have

$$-r_{i}\left[\check{f}_{mi}\left(\dot{q}_{mi}\right) + \rho_{f_{mi}} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] \leq \rho_{f_{mi}} r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}, \\ -\frac{1}{N_{i}} \cdot r_{i}\left[\tilde{\tau}ti + \rho_{\tau ti} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] \leq \frac{\rho_{\tau_{ti}}}{N_{i}}r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}, \\ -r_{i}\left[f_{qmi}\left(q_{mi},\dot{q}_{mi}\right) + \rho_{fqmi}sat\left(r_{i},\epsilon_{ri}\right)\right] \leq \rho_{fqmi}r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}, \\ -r_{i}\left[\tau_{basei} + I_{mi}\rho_{\alpha base} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] \leq I_{mi}\rho_{\alpha base}r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}.$$

$$(4.25)$$

Similarly, from Property 1, if $|r_i Y_{ij}(\dot{q}_{mi})| > \epsilon_{F_{mij}}$, the last item in Eq.(4.23) satisfies

$$-r_i Y_{ij}\left(\dot{q}_{mi}\right) \left[F_{mij}^v + \rho_{F_{mij}} sat\left(r_i Y_{ij}\left(\dot{q}_{mi}\right), \epsilon_{F_{mij}}\right)\right] < 0.$$

$$(4.26)$$

If $|r_i Y_{ij}(\dot{q}_{mi})| \leq \epsilon_{F_{mij}}$, we have

$$-r_{i}Y_{ij}\left(\dot{q}_{mi}\right)\left[F_{mij}^{v}+\rho_{F_{mij}}sat\left(r_{i}Y_{ij}\left(\dot{q}_{mi}\right),\epsilon_{F_{mij}}\right)\right]$$

$$\leq\rho_{F_{mij}}r_{i}Y_{ij}\left(\dot{q}_{mi}\right)\left\{\frac{r_{i}Y_{ij}(\dot{q}_{mi})}{|r_{i}Y_{ij}(\dot{q}_{mi})|}-\frac{r_{i}Y_{ij}(\dot{q}_{mi})}{\epsilon_{F_{mij}}}\right\}.$$

$$(4.27)$$

Since the right-side terms in Eq.(4.25) and Eq.(4.27) achieve the maximum values at $|r_i| = \frac{\epsilon_{ri}}{2}$

and $|r_i Y_{ij}(\dot{q}_i)| = rac{\epsilon_{F_{mij}}}{2}$, respectively, we can obtain

$$\dot{V} \le -I_{mi}\lambda_{i}r_{i}^{2} + \sum_{j=1}^{4} \frac{\rho_{F_{mij}}\epsilon_{F_{mij}}}{4} + \frac{\epsilon_{ri}}{4} \left(\rho_{f_{mi}} + \frac{\rho_{\tau_{ti}}}{N_{i}} + \rho_{f_{qmi}} + I_{mi}\rho_{\alpha base}\right).$$
(4.28)

From Eq.(4.28), V is a Lyapunov function only when

$$|r_{i}| > \sqrt{\frac{\frac{\epsilon_{ri}}{4} \left(\rho_{f_{mi}} + \frac{\rho_{\tau_{ti}}}{N_{i}} + \rho_{f_{qmi}} + I_{mi}\rho_{\alpha base}\right) + \sum_{j=1}^{4} \frac{\rho_{F_{mij}}\epsilon_{F_{mij}}}{4}}{I_{mi}\lambda_{i}}.$$
(4.29)

 $Define \ S = \left\{ r_i \in \Re \left| r_i^2 \le \frac{\frac{\epsilon_{ri} \left(\rho_{f_{mi}} + \frac{\rho_{\tau_{ti}}}{N_i} + \rho_{f_{qmi}} + I_{mi} \rho_{\alpha base} \right)}{2} + \sum_{j=1}^{4} \frac{\rho_{F_{mij}} \epsilon_{F_{mij}}}{2}}{I_{mi} \lambda_i} \right\}, \ on \ the \ surface \ of \ S,$ $\partial S, \ we \ have$

$$\dot{V} \leq -\left\{\frac{\epsilon_{ri}}{4}\left(\rho_{fi} + \frac{\rho_{\tau_{ti}}}{N_i} + \rho_{f_{qmi}} + I_{mi}\rho_{\alpha base}\right) + \sum_{j=1}^{4}\frac{\rho_{F_{mij}}\epsilon_{F_{mij}}}{4}\right\}.$$
(4.30)

Denote t_s as the time for the solution trajectory to intersect the surface ∂S , then

$$t_{s} \leq \frac{V(r_{i}(0)) - V(r_{i}(t_{s}))}{\frac{\epsilon_{ri}}{4} \left(\rho_{f_{mi}} + \frac{\rho_{\tau_{ti}}}{N_{i}} + \rho_{f_{qmi}} + I_{mi}\rho_{\alpha base}\right) + \sum_{j=1}^{4} \frac{\rho_{F_{mij}}\epsilon_{F_{mij}}}{4}.$$
(4.31)

Therefore, r_i is bounded, which indicates that e_i and \dot{e}_i are bounded as per the proof in (Slotine and Li 1991).

4.3 Interactive Force Compensation in Passive Mode

The proposed interactive force compensation technique is to make the joint move freely without generating excessive internal force. When a joint that is equipped with a mechanical clutch works in passive mode, the joint is totally free and will not generate any internal force. If the joint interactive forces can be controlled, then we can regulate the interactive forces to be around zero, and the joint will work in a virtual passive mode. It should be noted that the friction at the motor and transmission systems tends to prevent the compact wrist from

moving freely. Thus, friction compensation is essential to be taken into consideration. As the magnitude of constant friction dominates the total friction at low speeds, the friction can be substantially compensated by applying a feed-forward torque to the joint (Liu et al. 2008). Adapted from (Khatib 1995; Volpe and Khosla 1993), integrating the friction compensation torque with a proportional controller, the control law of robot-environment interactive force control can be given as

$$\tau_{mi} = \hat{f}_{mi}^c \left(q_{mi}, \dot{q}_{mi} \right) + \frac{\hat{\tau}_{ti}}{N_i} + \frac{\hat{I}_{mi} K_{pi} \left(\tau_{tid} - \hat{\tau}_{ti} \right)}{N_i}, \tag{4.32}$$

where $\hat{\tau}_{ti}$ is the estimated joint torque; τ_{tid} is the desired torque; and K_{pi} is a control parameter used for tuning; $\hat{f}_{mi}^c(q_{mi}, \dot{q}_{mi})$ is the joint's friction, which is calculated according to nominal friction parameters. In Eq.(4.32), the desired torque can be selected as $\tau_{tid} = 0$ for passive control. Substituting Eq.(4.32) into Eq.(4.6), if we neglect the uncertain part, we can obtain

$$K_{pi}^{-1}\ddot{q}_{mi} + \hat{\tau}_{ti} = 0. ag{4.33}$$

Eq.(4.33) indicates that the system behaves like a free body with inertia K_{pi}^{-1} .

4.4 Experiments

4.4.1 Motion Control with JTF

To demonstrate the efficiency of the proposed torque estimation method, an active control with the joint torque feedback as described in Eq.(4.19) was implemented using the experimental setup shown in Fig. 3.5(a). Joint 2, joint 3, and the link as described in Fig. 3.5(a) are used as payload. The distributed control method based on the joint torque feedback proposed in (Liu et al. 2006) is adopted in this dissertation as an application to demonstrate the effectiveness of the proposed joint torque estimation method. The design parameters and control parameters are detailed in Table 4.1. The results of the this experiment are presented in Fig. 4.2 and Fig. 4.3. Fig. 4.2 shows the desired position while the position error is shown in Fig. 4.3. In the first 20s of the experiment time, the joint torque feedback was set to zero and the link-side position error is shown in the area labeled (A) in Fig. 4.3. The link-side position error when using JTF from the F/T sensor is shown in area labeled (B), and the position error when using JTF with the estimated torque based on the proposed method is shown in area labeled (C).
Design and control parameters				Uncertainty bounds	
I_{m1}	$1.14\times10^{-5}kg.m^2$	ϵ_{Fmi1}	10^{-4}	ρ_{Fmi1}	10^{-3} (Nms/rad)
M2, M3	1.2 kg	ϵ_{Fmi2}	10^{-3}	ρ_{Fmi2}	10^{-2} (Nm)
Link length	0.45m	ϵ_{Fmi3}	10^{-3}	$ ho_{Fmi3}$	10^{-2} (Nm)
Link mass	0.64 kg	ϵ_{Fmi4}	0.10	ρ_{Fmi4}	1.0 (s^2/rad^2)
N_1	100	$\epsilon_{\dot{q}_{mi}}$	0.01	ρ_{base}	10^4 (rad/s ²)
λ_i	120	ϵ_{ri}	0.10	$ ho_{fqmi}$	2×10^{-3} (Nm)
K _{Ii}	10.0	μ_{Fic}	0.10	$ \rho_{\tau t i} $	1.0 (Nm)

Table 4.1: Design parameters and control parameters



Figure 4.2: Desired trajectory for active mode control



Figure 4.3: Active mode experimental results

In the second experiment, joint 3 is used as the payload, while joint 2 is controlled in position mode. Fig. 4.4 and Fig. 4.5 show the position and velocity of joint 2. Fig. 4.6 is joint 1's desired position trajectory. Fig. 4.8 and Fig. 4.7 show joint 1's position error at link side and motor side respectively. Fig. 4.9 shows the estimated torque using proposed method and F/T measured torque, and Fig. 4.10 shows the difference between the estimated torque using proposed method and F/T measured torque as estimated torque error.



Figure 4.4: Joint 2 position



Figure 4.5: Joint 2 velocity



Figure 4.6: Joint 1 desired position



Figure 4.7: Joint 1 motor side position error



Figure 4.8: Joint 1 link side position error



Figure 4.9: Joint 1 link side torque



Figure 4.10: Joint 1 link side torque estimation error

4.4.2 Passive Control

As another application of the joint torque feedback (JTF), a passive mode controller described as in Eq.(4.32) is implemented. The estimated joint torque as well as the F/T sensor measurements are used as JTF to the passive mode controller and the results are shown in Fig. 4.11. The joint was back-driven without joint torque feedback in the area labeled (A) in Fig. 4.11. The joint torque feedback with the estimated torque is shown in the area labeled (B), and the joint torque feedback with F/T sensor is shown in the area labeled (C).



Figure 4.11: Passive mode experimental results.

The joint angular position response is shown in Fig. 4.12.



Figure 4.12: Measured joint position for passive mode control

4.5 Conclusions

In this chapter, a multiple working mode control algorithm for modular and reconfigurable robot using proposed torque estimation technique is developed and experimentally tested. While working in active mode, the developed robust adaptive controller does not rely on a priori dynamic model and can suppress uncertainties caused by sensor inaccuracies and noises. With the proposed interactive force compensation technique, the joint can move freely without generating excessive internal force. The developed multiple mode control algorithm makes the modular and reconfigurable robot capable of working in sophisticated environments, such as door opening. The experimental results have verified the proposed multiple mode control algorithm with proposed torque estimation.

Chapter 5

Mechanism Structure and Kinematic Modeling of the Compact Wrist

Up to now extensive research has been reported on robot hand in various relevant fields such as mechanism design, grasping, manipulation, and control, etc. The inspiration for an anthropomorphic mechanism may be obtained via careful observations as well as the analysis of the human motion, whereas the obtained concept should be realized in the actual design of a mechanism. However, the robot hands reported up to now do not seem to satisfy the requirements for the humanlike motion as shown in Fig. 5.1. In case of the human hand, the dorsal and palm sides are obviously discriminated in terms of the motion it generates. For instance while grasping an object, only the palm side of the finger is utilized, not the dorsal one where the fingernail is located. However, the robot hands currently do not seem to reflect those observations. In this chapter, we will review a double active universal joint wrist mechanism that makes it possible to generate humanlike two-degree of freedom (DOF) motions, and derive the kinematic model by motion analysis and kinematic analysis. Inverse kinematics, differential kinematics and force analysis will be presented.



Figure 5.1: Swiveling of index finger and anthropomorphic motion

5.1 Mechanism Structure and Motion Analysis

To mimic the humanlike motion, a double active joint(DAUJ) wrist is developed in our laboratory. The 3D view, structure and assembly of the designed anthropomorphic wrist are shown in Fig. 5.2 and Fig. 5.3, respectively.

As shown in Fig. 5.3, the compact wrist consists mainly of a chassis, an internal inclined joint, two semi-spheres, two universal joints, two extended shafts, two pairs of gear boxes and two geared DC motors. The internal inclined joint controls the wrists rotation. Motor 1 is used to drive the lower semi-sphere through gearbox 1. The motion and force of Motor 2 are transmitted to the upper semi-sphere through gearbox 2, the two extended shafts as well as the inner universal joint. The outer universal joint is used to connect the input side link with the output side one and to prevent relative motion between them. Motion of the wrist is determined by the combination of the two semi-spheres. Comparing with the conventional wrist with two degrees of freedom, the developed wrist is more compact, as shown in Fig. 5.3.

Fig. 5.4 shows the simplified schematic diagram of the proposed anthropomorphic joint. J_i and q_i denote the *i*th joint and joint angle respectively. l_i is the distance between the preferred



Figure 5.2: 3D view of DAUJ joint with pitch and yaw motion



Figure 5.3: Structure of DAUJ joint



Figure 5.4: Kinematic diagram

joints. L_1 and L_2 represent the links of the anthropomorphic joint. In the proposed mechanism, the joint J_1 and J_2 are active joints driven by the geared DC motor with reduction mechanism and encoder used for position measurement. The outer and the inner universal joints in the figure represented by the joint couples, J_5 , J_6 and J_7 , J_8 , respectively, are passive joints. The joint J_4 is inclined at an angle ϕ , and two passive universal joints around J_4 prevent the relative motions between link L_1 and L_2 from rolling along the link axis. Joint J_3 is driven by Joint J_2 through the inner universal joint. From the simplified schematic diagram, if we define θ_2 as the angle of rotation for joint J_2 , θ_3 as the angle of rotation for joint J_3 , β as the bending angle of the universal joint or the angle of the axles with respect to each other, for a standard universal joint, we have

$$\theta_2 = atan2(\cos\beta\sin\theta_3, \cos\theta_3),\tag{5.1}$$

$$\omega_2 = \frac{\omega_3 \cos\beta}{\cos^2\theta_3 + \cos^2\beta \sin^2\theta_3},\tag{5.2}$$



$$\tau_2 = \frac{\cos^2\beta \sin^2\theta_3 + \cos^2\theta_3}{\cos\beta}\tau_3.$$
(5.3)

Figure 5.5: Workspace

The proposed workspace is shown in Fig. 5.5. The center of the sphere is the center of the two degrees rotation, and S is the end of the second link L_2 . The generation of the total workspace illustrated in Fig. 5.5 is explained as follows: if we fix θ_1 and change θ_4 , we obtain the workspace of a small cone represented in Fig. 5.5. The large cone in Fig. 5.5 means the workspace obtained by varying θ_1 and θ_4 . So the total workspace becomes the large cone generated by rotating the outer edge of the small cone slanted at the angle 2ϕ . In this figure, α and β denote longitudinal and latitudinal angles, δ and γ denote pitch and yaw angles, respectively.

Choi and Ryew (2000, 2000, 2001) proved the characteristics of the free of rolling and give the basic kinematics analysis and force analysis about this anthropomorphic joint. But the provided formula is based on polar coordinate system. It cannot be used directly and need to be modified for some application tasks based on Cartesian coordinate system. In our new manipulator, we need to know not only the direct forward kinematics (from the motor angle θ_1 and θ_3 to the output angles δ (Pitch) and γ (Yaw) of the outer universal joint) and their inverse kinematics, but also the direct force relationship between the motor torque τ_1 , τ_3 and the outer universal joint torques τ_{δ} and τ_{γ} at local Cartesian coordinate system.

Choi and Ryew (2000) gives the forward kinematics and their inverse kinematics between θ_1 , θ_3 , θ_4 and δ , γ . Since the structure of universal joint only allows two degrees of freedom (δ and γ), the three joint variables θ_1 , θ_3 and θ_4 are not independent and thus, θ_4 should be obtained from a function of θ_1 and θ_3 . But the relationship is not provided. In his following work (Ryew and Choi 2001), it is said that it is too complicated to get a solution.

Ryew (2000) uses a middle variable θ'_4 denotes the difference between the active rotations θ_3 and θ_1 ($\theta'_4 = \theta_3 - \theta_1$). It gives the forward kinematics and their inverse kinematics between θ_1 , θ_3 and α , β . The output α and β are not our needed variables δ and γ .

Ryew (2000) provides the forward and inverse kinematics between θ_1 , θ_3 and α , β . Similarly, the outputs are not our expected angles δ and γ . On the other hand, only (Ryew et al. 2000) analyzes the force relationship. But it is also the relationship between the motor torques τ_1 , τ_3 and the torques in polar coordinate system τ_{α} , τ_{β} . What we need is the relationship between the motor torque τ_1 , τ_2 and the outer universal joint torques τ_{δ} and τ_{γ} at local Cartesian coordinate system. In order to satisfy the application requirements, the following kinematics analysis and force analysis provide a final complete solution.

5.2 Anthropomorphic Wrist Kinematic Analysis

Anthropomorphic wrist has an internal oblique joint which controls the joint rotation. It consists of an upper and a lower semi sphere that meet each other in an inclined plane with an angle ϕ as illustrated in Fig. 5.4, Fig. 5.6 describes the kinematics parameters and the coordinate frame assignments for the proposed mechanism. The coordinate frame Σ_2 is assigned to the internal oblique joint; the global coordinate frame Σ_0 is fixed to the base of the mechanism.

In path 1, from Σ_0 to Σ_3 , there exists the following homogeneous transform matrix.

$$T_{03}(\theta_1, \theta_4, \theta_3) = T_{01s} T_{1m} T_{14s} T_{4m} T_{43s} T_{3m}$$

= $T_z(\theta_1) T_x(-\phi) T_z(\theta_4) T_x(\phi) T_z(\theta_3),$ (5.4)



Figure 5.6: Kinematics parameters and frame assignment

$$T_{03}(\theta_{1},\theta_{4},\theta_{3}) = \begin{vmatrix} C_{1} & -S_{1} & 0 & 0 \\ S_{1} & C_{1} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix} \cdot \begin{vmatrix} 1 & 0 & 0 & 0 \\ 0 & C_{\phi} & -S_{\phi} & 0 \\ 0 & S_{\phi} & C_{\phi} & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

$$= \begin{vmatrix} C_{4} & -S_{4} & 0 & 0 \\ S_{4} & C_{4} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix} \cdot \begin{vmatrix} 1 & 0 & 0 & 0 \\ 0 & C_{\phi} & S_{\phi} & 0 \\ 0 & -S_{\phi} & C_{\phi} & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix} \cdot \begin{vmatrix} C_{3} & -S_{3} & 0 & 0 \\ S_{3} & C_{3} & 0 & 0 \\ S_{3} & C_{3} & 0 & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

$$= \begin{vmatrix} t_{11} & t_{12} & t_{13} & t_{14} \\ t_{21} & t_{22} & t_{23} & t_{24} \\ t_{31} & t_{32} & t_{33} & t_{34} \\ t_{41} & t_{42} & t_{43} & t_{44} \end{vmatrix},$$
(5.5)

where S_i represents $\sin \theta_i$, C_i represents $\cos \theta_i$, S_{ϕ} represents $\sin \phi$, C_{ϕ} represents $\cos \phi$ and

$$\begin{split} t_{11} &= C_1 C_4 C_3 - S_1 S_4 C_3 C_{\phi} - C_1 S_4 S_3 C_{\phi} - S_1 C_4 S_3 C_{\phi}^2, \\ t_{21} &= S_1 C_4 C_3 + C_1 S_4 C_3 C_{\phi} - S_1 S_4 S_3 C_{\phi} + C_1 C_4 S_3 C_{\phi}^2 + C_1 S_3 S_{\phi}^2, \\ t_{31} &= -S_3 C_{\phi} S_{phi} + S_4 C_3 S_{\phi} + C_4 S_3 S_{\phi} C_{phi}, \\ t_{41} &= 0, \\ t_{12} &= S_1 S_4 S_3 C_{\phi} - C_1 C_4 S_3 - C_1 S_4 C_3 C_{\phi} - S_1 C_4 C_3 C_{\phi}^2 - S_1 S_3 S_{\phi}^2, \\ t_{22} &= C_1 C_4 C_3 C_{\phi}^2 + C_1 C_3 S_{\phi}^2 - S_1 C_4 S_3 - C_1 S_4 S_3 C_{\phi} - S_1 S_4 C_3 C_{\phi}, \\ t_{32} &= -S_4 S_3 S_{\phi} - C_3 C_{\phi} S_{\phi} + C_4 C_3 S_{\phi} C_{\phi}, \\ t_{42} &= 0, \\ t_{13} &= S_1 C_{\phi} S_{\phi} - C_1 S_4 S_{\phi} - S_1 C_4 C_{\phi} S_{\phi}, \\ t_{23} &= C_1 C_4 C_{\phi} S_{\phi} - S_1 S_4 S_{\phi} - C_1 C_{\phi} S_{\phi}, \\ t_{43} &= 0, \\ t_{14} &= 0, \\ t_{14} &= 0, \\ t_{24} &= 0, \\ t_{14} &= 0, \\ t_{24} &= 0, \\ t_{34} &= 0, \\ t_{44} &= 1. \end{split}$$

For the outer universal joint, variables δ (pitch) and γ (yaw) are assigned in coordinate frame Σ_6 and Σ_5 , respectively. Then, from Σ_0 to Σ_3 , there is a homogeneous transform matrix as follows.

$$T_{03}(\delta,\gamma) = T_y(\delta)T_x(\gamma)$$

$$= \begin{vmatrix} C_{\delta} & 0 & S_{\delta} & 0 \\ 0 & 1 & 0 & 0 \\ -S_{\delta} & 0 & C_{\delta} & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix} \begin{vmatrix} 1 & 0 & 0 & 0 \\ 0 & C_{\gamma} & -S_{\gamma} & 0 \\ 0 & S_{\gamma} & C_{\gamma} & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$
(5.6)

$$= \begin{vmatrix} C_{\delta} & S_{\delta}S_{\gamma} & C_{\gamma}S_{\delta} & 0 \\ 0 & C_{\gamma} & -S_{\gamma} & 0 \\ -S_{\delta} & C_{\delta}S_{\gamma} & C_{\delta}C_{\gamma} & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix},$$

where S_{γ} represents $\sin \gamma$, C_{γ} represents $\cos \gamma$, S_{δ} represents $\sin \delta$, C_{δ} represents $\cos \delta$. The transformation matrix from Σ_0 to Σ_3 is able to derived in two different paths, path 1 and path 2 shown in Fig. 5.6. So the result should satisfy the relationship as followings:

$$T_{03}(\delta,\gamma) = T_{03}(\theta_1,\theta_4,\theta_3)$$
(5.7)

From Eq.(5.7), it can be assured that none of the three joint variables θ_1 , θ_4 , and θ_3 are independent. θ_1 , θ_4 , and θ_3 should satisfy following relationship:

$$t_{21} = S_1 C_4 C_3 + C_1 S_4 C_3 C_\phi - S_1 S_4 S_3 C_\phi + C_1 C_4 S_3 C_\phi^2 + C_1 S_3 S_\phi^2 = 0.$$
(5.8)

From Eq.(5.8), we get

$$C_4(S_1C_3 + C_1S_3C_{\phi}^2) + S_4(C_1C_3C_{\phi} - S_1S_3C_{\phi}) = -C_1S_3S_{\phi}^2.$$
(5.9)

Solve Eq.(5.9), we can get

$$\theta_4 = a \pm \arccos(-\frac{C_1 S_3 S_\phi^2}{b}),\tag{5.10}$$

where

$$a = \arctan 2(C_{13}C_{\phi}, S_1C_3 + C_1S_3C_{\phi}^2),$$

$$b = \sqrt{(S_1C_3 + C_1S_3C_{\phi}^2)^2 + C_{13}^2C_{\phi}^2},$$

$$C_{13} = \cos(\theta_1 + \theta_3).$$

Given θ_1 and θ_3 , we can calculate θ_4 . Therefore we can obtain δ and γ from t_{11} , t_{31} , t_{22} , and

 t_{23} as follows.

$$\delta = \arctan 2(-C_4 S_3 S_{\phi} C_{\phi} + S_3 C_{\phi} S_{\phi} - S_4 C_3 S_{\phi},$$

$$C_1 C_4 C_3 - S_1 S_4 C_3 C_{\phi} - C_1 S_4 S_3 C_{\phi} - S_1 C_4 S_3 C_{\phi}^2 - S_1 S_3 S_{\phi}^2)$$

$$\gamma = \arctan 2(-C_1 C_4 C_{\phi} S_{\phi} + S_1 S_4 S_{\phi} + C_1 C_{\phi} S_{\phi},$$

$$C_1 C_4 C_3 C_{\phi}^2 + C_1 C_3 S_{\phi}^2 - S_1 C_4 S_3 - C_1 S_4 S_3 C_{\phi} - S_1 S_4 C_3 C_{\phi})$$
(5.11)

Mathematically, there are two sets of solution. But physically there should be only one set of correct solution. We define the initial status as $\theta_1 = \theta_3 = 0$, $\delta = \gamma = 0$. From observations, we know when $\theta_1 = 1$ and θ_3 =-1, δ and γ should keep to zero. When $\theta_4 = a + \arccos(-\frac{C_1 S_3 S_{\phi}^2}{b})$, from Eq.(5.11), we can get δ =-2.6681 and γ =2.8342. Similarly when $\theta_4 = a - \arccos(-\frac{C_1 S_3 S_{\phi}^2}{b})$, we can get δ =0 and γ =0.

So the correct solution is:

$$\theta_4 = a - \arccos(-\frac{C_1 S_3 S_{\phi}^2}{b}).$$
(5.12)

5.3 Inverse Kinematic Analysis

For the inverse kinematics, from t_{33} , we have

$$\theta_4 = \pm \arccos(\frac{C_\delta C_\gamma - C_\phi^2}{S_\phi^2}). \tag{5.13}$$

From

$$\begin{split} t_{13} &= S_1 C_{\phi} S_{\phi} - C_1 S_4 S_{\phi} - S_1 C_4 C_{\phi} S_{\phi} = C_{\gamma} S_{\delta}, \\ t_{23} &= C_1 C_4 C_{\phi} S_{\phi} - S_1 S_4 S_{phi} - C_1 C_{\phi} S_{\phi} = -S_{\gamma}, \end{split}$$

we can get

$$S_{1} = \frac{(1 - C_{4})C_{\phi}S_{\phi}C_{\gamma}S_{\delta} + S_{4}S_{\phi}S_{\gamma}}{S_{4}^{2}S_{\phi}^{2} + (C_{4} - 1)^{2}C_{\phi}^{2}S_{\phi}^{2}},$$
$$C_{1} = \frac{(1 - C_{4})C_{\phi}S_{\phi}S_{\gamma} - C_{\gamma}C_{\delta}S_{4}S_{\phi}}{S_{4}^{2}S_{\phi}^{2} + (C_{4} - 1)^{2}C_{\phi}^{2}S_{\phi}^{2}}.$$

Therefore,

$$\theta_1 = \arctan 2((1 - C_4)C_{\phi}S_{\phi}C_{\gamma}S_{\delta} + S_4S_{\phi}S_{\gamma}, (1 - C_4)C_{\phi}S_{\phi}S_{\gamma} - C_{\gamma}C_{\delta}S_4S_{\phi}).$$

Same as above, from

$$t_{31} = S_3 C_{\phi} S_{\phi} + S_4 C_3 S_{\phi} - C_4 S_3 S_{\phi} C_{\phi} = -S_{\delta},$$

$$t_{32} = S_4 S_3 S_{\phi} - C_3 C_{\phi} S_{\phi} + C_4 C_3 S_{phi} C_{\phi} = C_{\delta} S_{\gamma},$$

we can also obtain

$$C_{3} = -\frac{(1 - C_{4})C_{\phi}S_{\phi}S_{\gamma}C_{\delta} + S_{4}S_{\phi}S_{\delta}}{S_{4}^{2}S_{\phi}^{2} + (C_{4} - 1)^{2}C_{\phi}^{2}S_{\phi}^{2}},$$

$$S_{3} = \frac{(1 - C_{4})C_{\phi}S_{\phi}S_{\delta} - C_{\delta}S_{\gamma}S_{2}S_{\phi}}{S_{4}^{2}S_{\phi}^{2} + (C_{4} - 1)^{2}C_{\phi}^{2}S_{\phi}^{2}}.$$

Therefore,

$$\theta_3 = \arctan 2((1 - C_4)C_{\phi}S_{\phi}S_{\delta} - C_{\delta}S_{\gamma}S_4S_{\phi}, -(1 - C_4)C_{\phi}S_{\phi}S_{\gamma}C_{\delta} - S_4S_{\delta}S_{\phi}).$$

For only positive direction of θ_4 , the inverse kinematics becomes Eq.(5.14)

$$\theta_{4} = \arccos(\frac{C_{\delta}C_{\gamma} - C_{\phi}^{2}}{S_{\phi}^{2}}),$$

$$\theta_{1} = \arctan 2((1 - C_{4})C_{\phi}S_{\phi}C_{\gamma}S_{\delta} + S_{4}S_{\phi}S_{\gamma}, (1 - C_{4})C_{\phi}S_{\phi}S_{\gamma} - C_{\gamma}C_{\delta}S_{4}S_{\phi}),$$

$$\theta_{3} = \arctan 2((1 - C_{4})C_{\phi}S_{\phi}S_{\delta} - C_{\delta}S_{\gamma}S_{4}S_{\phi}, -(1 - C_{4})C_{\phi}S_{\phi}S_{\gamma}C_{\delta} - S_{4}S_{\delta}S_{\phi}).$$
(5.14)

For all possible δ and γ , we can get θ_1 and θ_3 . Fig. 5.7 shows their mapping. We find for continuous δ and γ , it's possible to get discontinuous θ_1 and θ_3 . So we need to modify Eq.(5.14) to Eq.(5.15)

$$\theta_{3} = \arctan 2((1 - C_{4})C_{\phi}S_{\phi}S_{\delta} - C_{\delta}S_{\gamma}S_{4}S_{\phi}, -(1 - C_{4})C_{\phi}S_{\phi}S_{\gamma}C_{\delta} - S_{4}S_{\delta}S_{\phi}) + 2\mu\pi,$$

$$\mu = \{ \begin{array}{cc} 0 & \theta_{1} + \theta_{3} \ge -\pi/2 \\ 1 & \theta_{1} + \theta_{3} < -\pi/2. \end{array}$$
(5.15)



Figure 5.7: Workspace mapping

Then, the mapping becomes Fig. 5.8.



Figure 5.8: Adjusted workspace mapping

Fig. 5.9 is an equivalent kinematic diagram by omitting the inner universal joint. In the derivation of Z-Y-Z Euler angle description is employed to exploit the characteristic of the mechanism. According to Z-Y-Z Euler angle representation, the rotation of the joint can be considered to perform in the following order: rotation about Z axis by α , rotation about negative Y' axis



Figure 5.9: Generalized coordinate frame assignment

by β , and rotation about Z" axis by $-\alpha'$, which gives the transformation matrix as Eq.(5.16)

$$= \begin{vmatrix} C_{\alpha}C_{beta}C_{\alpha'} + S_{\alpha}S_{\alpha'} & C_{\alpha}S_{\alpha'} - S_{\alpha}C_{beta}C_{\alpha'} & S_{\beta}C_{alpha'} & 0 \\ S_{\alpha}C_{\alpha'} - C_{\alpha}C_{beta}S_{\alpha'} & C_{\alpha}C_{\alpha'} + S_{\alpha}C_{beta}S_{\alpha'} & -S_{\beta}S_{\alpha'} & 0 \\ -C_{\alpha}S_{\beta} & S_{\alpha}S_{\beta} & C_{\beta} & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix},$$
(5.16)

where S_{α} represents $\sin \alpha$, C_{α} represents $\cos \alpha$, S_{β} represents $\sin \beta$, C_{β} represents $\cos \beta$. Because

$$T(\alpha,\beta) = T(\theta_1,\theta_4,\theta_3),$$

from

$$t_{33} = C_\beta = C_2 S_\phi^2 + C_\phi^2,$$

we can get

$$\beta = \arccos(C_2 S_{\phi}^2 + C_{\phi}^2), \tag{5.17}$$

where

$$\theta_{4} = a - \arccos - \frac{C_{1}S_{3}S_{\phi}^{2}}{b},$$

$$a = \arctan 2(C_{13}C_{\phi}, S_{1}C_{3} + C_{1}S_{3}C_{\phi}^{2}),$$

$$b = \sqrt{(S_{1}C_{3} + C_{1}S_{3}C_{\phi}^{2})^{2} + C_{13}^{2}C_{\phi}^{2}},$$

$$C_{13} = \cos(q_{1} + q_{3}).$$
(5.18)

From

$$t_{31} = -S_3 C_{\phi} S_{\phi} + S_4 C_3 S_{\phi} + C_4 S_3 S_{\phi} C_{\phi} = -C_{\alpha} S_{\beta},$$

$$t_{32} = -S_4 S_3 S_{\phi} - C_3 C_{\phi} S_{\phi} + C_4 C_3 S_{\phi} C_{\phi} = S_{\alpha} S_{\beta},$$

we can also get

$$\alpha = \arctan 2(-S_4 S_3 - C_3 C_\phi + C_4 C_3 C_\phi, -C_4 S_3 C_\phi + S_3 C_\phi - S_4 C_3).$$
(5.19)

The relationships between θ_1 , θ_3 and α , β are also derived by Sungmoo Ryew and Hyoukryeol Choi [2001] as follows:

$$\alpha = \frac{\theta_1 + \theta_3}{2} + \pi,$$

$$\beta = 2 \arctan(\tan\phi\cos\frac{\theta_3 - \theta_1}{2}).$$
(5.20)

However, Eq.(5.18) is an approximation of the relationship between θ_1 , θ_3 and α , β , because it assumed α' equal to α when the relationship is derived. If we choose the same direction and initialization, Eq.(5.20) becomes Eq.(5.21)

$$\alpha = \frac{\theta_1 - \theta_3}{2},$$

$$\beta = 2 \arctan(\tan\phi\cos\frac{\theta_3 + \theta_1}{2}).$$
(5.21)

Fig. 5.10 and Fig. 5.11 show the comparison between Eq.(5.17), Eq.(5.19) and Eq.(5.21).



Figure 5.10: Difference between two α solutions



Figure 5.11: Difference between two β solutions

5.4 Differential Kinematics and Force Analysis

Because the difference between Eq.(5.17), Eq.(5.19) and Eq.(5.21) is less than 2%, we still use Sungmoo Ryew and Hyoukryeol Choi's solution in Force analysis. Taking derivatives of Eq.(5.21), we get

$$\dot{\alpha} = \frac{\dot{\theta}_1 - \dot{\theta}_3}{2},$$

$$\dot{\beta} = -\Omega(\dot{\theta}_1 - \dot{\theta}_3),$$
(5.22)

where

$$\Omega = \frac{\sin\frac{\theta_1 - \theta_3}{2}\tan\phi}{1 + \cos^2\frac{\theta_1 - \theta_3}{2}\tan^2\phi}.$$

If we define

$$\dot{q} = [\dot{\theta}_1, \dot{\theta}_3]^T,$$

$$\omega = [\dot{\alpha}, \dot{\beta}]^T,$$

$$\omega = J_c \dot{q},$$

(5.23)

then

$$J_c = \begin{vmatrix} \frac{1}{2} & \frac{1}{2} \\ -\Omega & \Omega \end{vmatrix}.$$
 (5.24)

The relationship between τ_{13} and $\tau_{\alpha\beta}$ can be expressed as

$$\tau_{13} = J_c^T \tau_{\alpha\beta},$$

$$\tau_{\alpha\beta} = (J_c^T)^{-1} \tau_{13}.$$
(5.25)

For δ and γ , we also have

$$\begin{bmatrix} \dot{\delta} \\ \dot{\gamma} \end{bmatrix} = J_2 \begin{bmatrix} \dot{\alpha} \\ \dot{\beta} \end{bmatrix}, \qquad (5.26)$$

where

$$J_{2} = \begin{bmatrix} \frac{-\tan\beta\sin\alpha}{1+\tan^{2}\beta\cos\alpha} & \frac{-\sec^{2}\beta\cos\alpha}{1+\tan^{2}\beta\cos^{2}\alpha} \\ \frac{\tan\beta\cos\alpha}{1+\tan^{2}\beta\sin\alpha} & \frac{\sec^{2}\beta\sin\alpha}{1+\tan^{2}\beta\sin^{2}\alpha} \end{bmatrix}.$$
 (5.27)

According to the principle of virtual work, we can obtain following relationships between forces:

$$\begin{bmatrix} \tau_1 \\ \tau_3 \end{bmatrix} = J_c^T J_2^T \begin{bmatrix} \tau_\delta \\ \tau_\gamma \end{bmatrix},$$
(5.28)

$$\begin{bmatrix} \tau_{\delta} \\ \tau_{\gamma} \end{bmatrix} = (J_c^T)^{-1} (J_2^T)^{-1} \begin{bmatrix} \tau_1 \\ \tau_3 \end{bmatrix}.$$
 (5.29)

Chapter 6

Multiple Mode Control of the Compact Wrist

In this chapter, a multiple mode control method is developed for the compact wrist, making it work in active mode with position or torque control, or passive mode with interactive force compensation. A robust adaptive control algorithm is developed for motion control of the compact wrist in active mode; and an interactive force compensation technique is proposed to make it capable of working in passive mode.

6.1 Robust Adaptive Control in Active Mode

As derived in last chapter, the wrist-environment interactive forces can be mapped from task space into joint space as follows:

$$\begin{bmatrix} \tau_{t1} \\ \tau_{t2} \end{bmatrix} = J \cdot \begin{bmatrix} \tau_{\delta} \\ \tau_{\gamma} \end{bmatrix}$$
(6.1)

$$J = J_c^T J_2^T \tag{6.2}$$

where τ_{t1} and τ_{t2} denote torques exerted to the joints due to the interactive forces between the wrist and the environment; the Jacobian matrix $J_c J_2$ are as shown in Eq.(5.24) and Eq.(5.27); τ_{δ} and τ_{γ} represent interactive torques that contribute to the roll and yaw motions of the wrist,

which can be derived from the force/torque sensor measurements as follows:

$$\begin{bmatrix} \tau_{\delta} \\ \tau_{\gamma} \end{bmatrix} = \begin{bmatrix} 0 & -l\cos\gamma & 0 & 1 & 0 & -\sin\gamma \\ -l & 0 & 0 & 0 & -1 & 0 \end{bmatrix} \cdot \begin{bmatrix} F_x \\ F_y \\ F_z \\ \tau_x \\ \tau_y \\ \tau_z \end{bmatrix}$$
(6.3)

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where F_x , F_y , F_z , τ_x , τ_y and τ_z are measurements of the force/torque sensor, as shown in Fig. 6.1; and l is the distance between the force/torque sensor and the center of the wrist, as shown in Fig. 6.1.



Figure 6.1: Force sensor installation and coordinate system definition

The light-weight compact wrist is normally integrated with a robotic arm. With the assumption that the compact wrist is mounted on a series robotic arm with n rotary joints, the dynamics of the compact wrist can be described by (Liu et al. 2008):

$$I_{mi}N_{i}\ddot{q}_{i} + f_{i}(q_{i},\dot{q}_{i}) + I_{mi}\sum_{j=1}^{n} z_{mi}^{T} z_{lj}\ddot{q}_{lj} + I_{mi}\sum_{j=2}^{n}\sum_{k=1}^{j-1} z_{mi}^{T} \left(z_{lk} \times z_{lj} \right) \dot{q}_{lk}\dot{q}_{lj} + \frac{\tau_{ti}}{N_{i}} = \tau_{mi}$$
(6.4)

where $i \in \{1, 2\}$; I_{mi} is the moment of inertia about the axis of rotation; N_i denotes the gear ratio (including the gear heads and gear boxes); τ_{ti} is the torque caused by wrist-environment interactions, as detailed in Eq.(6.1); z_{mi} is a unit vector along the axis of rotation of the i_{th} rotor; z_{li} is the unity vector along the axis of rotation of joint i; τ_{mi} is output torque of the i_{th} motor; $\dot{\theta}_{lj}$, $\dot{\theta}_{lk}$ and $\ddot{\theta}_{lj}$ represent joint angular velocities and acceleration of the base robotic arm; $f_i(q_i, \dot{q}_i)$ represents the joint's friction, which can be modeled as a function of the joint position and velocity as follows (Armstrong-Helouvry et al. 1994):

$$f_i(q_i, \dot{q}_i) = \left[f_{ci} + f_{si} \exp\left(- f_{\tau i} \dot{q}_i^2 \right) \right] sgn\left(\dot{q}_i \right) + b_i \dot{q}_i + f_{qi}\left(q_i, \dot{q}_i \right)$$
(6.5)

where f_{ci} are Coulomb friction related parameters; f_{si} are static friction related parameters; $f_{\tau i}$ are positive parameters corresponding to the Stribeck effect; b_i are viscous friction coefficients; and $f_{qi}(q_i, \dot{q}_i)$ are position dependency of friction and other friction modeling errors; $sgn(\dot{q}_i)$ is the signum function as defined in Eq.(2.17).

Let $F_i = [b_i f_{ci} f_{si} f_{\tau i}]^T$. According to the model uncertainty decomposition scheme proposed in (Liu et al. 2006), F_i

can be decomposed into a constant part plus a variable part, i.e.,

$$F_i = F_i^c + F_i^v \tag{6.6}$$

where the superscripts "c" and "v" represent constant and variable part, respectively.

Property 2 *The variable part in Eq.*(6.6) *is bounded, i.e.,*

$$|F_i^v| < \rho_{Fi} \tag{6.7}$$

where ρ_{Fi} is constant bound.

Assumption 7 The nonparametric friction term in Eq.(6.5) is bounded, i.e.,

$$|f_{qi}(q_i, \dot{q}_i)| < \rho_{fqi} \tag{6.8}$$

where is a known constant bound for any positions q_i and velocities \dot{q}_i .

Assumption 8 Since z_{mi} , z_{lj} and z_{lk} are unit vectors, the resulting vector products $z_{mi}^T(z_{lk} \times z_{lj})$ and $z_{mi}^T z_{lj}$ are bounded. Furthermore, as the base robotic arm is stabilized, the accelerations $(\ddot{\theta}_{lj})$ and velocities $(\dot{\theta}_{lj}, \dot{\theta}_{lk})$ of the robotic arm joints must be bounded. Hence, the inertial and Coriolis forces associated with motion of the base robotic arm are bounded, i.e., if

$$\rho_{\alpha_{base}} > max \left| \sum_{j=1}^{n} z_{mi}^{T} z_{lj} \ddot{\theta}_{lj} + \sum_{j=2}^{n} \sum_{k=1}^{j-1} z_{mi}^{T} \left(z_{lk} \times z_{lj} \right) \dot{\theta}_{lk} \dot{\theta}_{lj} \right|$$
(6.9)

for any possible configuration, then

we define

$$|\tau_{basei}| = I_{mi} \left| \sum_{j=1}^{n} z_{mi}^{T} z_{lj} \ddot{\theta}_{lj} + \sum_{j=2}^{n} \sum_{k=1}^{j-1} z_{mi}^{T} \left(z_{lk} \times z_{lj} \right) \dot{\theta}_{lk} \dot{\theta}_{lj} \right| < I_{mi} \rho_{base}, \tag{6.10}$$

where ρ_{base} is a constant bound.

Assumption 9 The force/torque sensor inaccuracy and noise is bounded; furthermore, the estimate errors of τ_{δ} , τ_{γ} and τ_{ti} are bounded, i.e.,

$$\begin{aligned} |\tilde{\tau}_{\delta}| &= |\tau_{\delta} - \hat{\tau}_{\delta}| < \rho_{\tau\delta} \\ |\tilde{\tau}_{\gamma}| &= |\tau_{\gamma} - \hat{\tau}_{\gamma}| < \rho_{\tau\gamma} \\ |\tilde{\tau}_{ti}| &= |\tau_{ti} - \hat{\tau}_{ti}| < \rho_{\tau ti} \end{aligned}$$
(6.11)

where $\hat{\tau}_{\delta}$, $\hat{\tau}_{\gamma}$ and τ_{ti} are derived from Eq.(6.1) and Eq.(6.3) with the force/torque sensor measurements; $\rho_{\tau\delta}$, $\rho_{\tau\gamma}$ and $\rho_{\tau ti}$ are known constant bounds.

Define the system errors as

$$e_{i} = q_{i} - q_{id}$$

$$r_{i} = \dot{e}_{i} + \lambda_{i}e_{i}$$

$$a_{i} = \ddot{q}_{id} - 2\lambda_{i}\dot{e}_{i} - \lambda_{i}^{2}e_{i}$$
(6.12)

where q_{id} is the desired joint space motion for the i_{th} joint, which may be derived from the desired task-space rotations (δ_d, γ_d) with the inverse kinematics; \dot{q}_{id} denotes corresponding joint-space velocities, which can be derived from task-space velocities $(\dot{\delta}_d, \dot{\gamma}_d)$ with differential kinematics, or calculated by differentiating q_{id} ; \ddot{q}_{id} represents desired joint-space accelerations; λ_i is a positive constant.

Chapter 6

Let \hat{b}_{i}^{c} , \hat{f}_{ci}^{c} , \hat{f}_{si}^{c} and $\hat{f}_{\tau i}^{c}$ represent estimates of the constant friction parameters and by using the linearization scheme proposed in (Liu et al. 2006), the friction model shown in Eq.(6.5) can be approximated by

$$f_{i}(q_{i},\dot{q}_{i}) \approx \hat{f}_{i}^{c}(\dot{q}_{i}) + Y_{i}(\dot{q}_{i})\left(\tilde{F}_{i}^{c} + F_{i}^{v}\right) + f_{qi}(q_{i},\dot{q}_{i}) + \check{f}_{i}(\dot{q}_{i})$$
(6.13)

where $\tilde{F}_i^c = F_i^c - \hat{F}_i^c$ with $\hat{F}_i^c = [\hat{b}_i^c \ \hat{f}_{ci}^c \ \hat{f}_{si}^c \ \hat{f}_{\tau i}^c]^T$; $\hat{f}_i^c (\dot{q}_i)$, $\check{f}_i (\dot{q}_i)$, and $Y_i (\dot{q}_i)$ can be detailed as follows:

$$\begin{aligned}
f_{i}^{c}(\dot{q}_{i}) &= \left[f_{ci}^{c} + f_{si}^{c} \exp\left(- \bar{f}_{\tau i}^{c} \dot{q}_{i}^{2} \right) \right] sat\left(\dot{q}_{i}, \epsilon_{\dot{q}_{i}} \right) + \bar{b}_{i}^{c} \dot{q}_{i} \\
\check{f}_{i}(\dot{q}_{i}) &= \left[f_{ci} + f_{si} \exp\left(- f_{\tau i} \dot{q}_{i}^{2} \right) \right] \left[sgn\left(\dot{q}_{i} \right) - sat\left(\dot{q}_{i}, \epsilon_{\dot{q}_{i}} \right) \right] \\
Y_{i}(\dot{q}_{i}) &= \left[0 \ 1 \ \exp\left(- \hat{f}_{\tau i}^{c} \dot{q}_{i}^{2} \right) - \hat{f}_{si}^{c} \dot{q}_{i}^{2} \exp\left(- \hat{f}_{\tau i}^{c} \dot{q}_{i}^{2} \right) \right] \\
\cdot sat(\dot{q}_{i}, \epsilon_{\dot{q}_{i}}) + \left[\dot{q}_{i} \ 0 \ 0 \ 0 \right]
\end{aligned}$$
(6.14)

where $\epsilon_{\dot{q}_i}$ is a positive constant, sat(x,y) is the saturation function as defined as Eq.(4.16).

Assumption 10 The last item in Eq.(6.13) $\check{f}_i(\dot{q}_i)$ is bounded, i.e., $|\check{f}_i(\dot{q}_i)| < \rho_{fi}$.

To follow the desired trajectories in joint space, a robust adaptive control law is designed as follows:

$$\tau_{mi} = I_{mi} N_i a_i + \frac{\hat{\tau}_{ti}}{N_i} + \hat{f}_i^c (\dot{q}_i) - K_{Ii} \int_0^t r_i (t) dt - \left(\rho_{fi} + \rho_{fqi} + I_{mi} \rho_{base} + \frac{\rho_{\tau ti}}{N_i}\right) \cdot sat (r_i, \epsilon_{ri}) - \sum_{j=1}^4 \left\{ \rho_{Fij} Y_{ij} (\dot{q}_i) sat (r_i Y_{ij} (\dot{q}_i), \epsilon_{Fij}) \right\}$$
(6.15)

where $Y_{ij}(\dot{q}_i)$ is the j_{th} element of $Y_i(\dot{q}_i)$, and ϵ_{ri} and ϵ_{Fij} are positive control parameters.

Theorem 2 Given the compact wrist with the joint dynamics as given in Eq.(6.4), the tracking error of each joint is uniformly ultimately bounded under the control law given by Eq.(6.15) and the adaption law of $\hat{F}_i^c = -\mu_{Fic} [Y_i(\dot{q}_i)]^T r_i$ with μ_{Fic} a positive constant.

proof 2 Consider the Lyapunov function candidate

$$V = \frac{1}{2} I_{mi} N_i r_i^2 + \frac{1}{2} k_{Ii} \left[\int_0^t r_i(t) dt \right]^2 + \frac{1}{2} \frac{\left(\tilde{F}_i^c\right)^T \tilde{F}_i^c}{\mu_{Fic}}$$
(6.16)

Differentiating Eq.(6.16) yields

$$\dot{V} = r_i \left\{ I_{mi} N_i \dot{r}_i + k_{Ii} \int_0^t r_i(t) dt \right\} + \frac{\left(\check{F}_i^c \right)^T \check{F}_i^c}{\mu_{Fic}}$$
(6.17)

Substituting Eq.(6.12) and Eq.(6.15) into Eq.(6.4) yields

$$r_{i}\left\{I_{mi}N_{i}\dot{r}_{i}+K_{Ii}\int_{0}^{t}r_{i}\left(t\right)dt\right\} = -I_{mi}N_{i}\lambda_{i}r_{i}^{2}-r_{i}f_{i}\left(q_{i},\dot{q}_{i}\right)-r_{i}\tau_{basei}$$

$$-r_{i}\left[\frac{\tilde{\tau}_{ti}+\rho_{\tau ti}sat(r_{i},\epsilon_{\tau i})}{N_{i}}\right]-r_{i}\left(\rho_{fi}+\rho_{fqi}+I_{mi}\rho_{base}\right)sat\left(r_{i},\epsilon_{\tau i}\right)$$

$$-r_{i}\sum_{j=1}^{4}\left\{\rho_{Fij}Y_{ij}\left(\dot{q}_{i}\right)\cdot sat\left(r_{i}Y_{ij}\left(\dot{q}_{i}\right),\epsilon_{Fij}\right)\right\}+r_{i}\hat{f}_{i}^{c}\left(\dot{q}_{i}\right)$$

$$(6.18)$$

Since F_i^c is a constant vector, we have $\dot{F}_i^c = -\dot{F}_i^c$. Substituting Eq.(6.18) and the adaption law into Eq.(6.17), with consideration of Eq.(6.13), we can obtain,

$$\dot{V} = -I_{mi}N_i\lambda_i r_i^2 - r_i \left[\check{f}_i\left(\dot{q}_i\right) + \rho_{fi}sat\left(r_i,\epsilon_{ri}\right)\right] - \frac{r_i \left[\check{\tau}_{ti} + \rho_{\tau ti}sat(r_i,\epsilon_{ri})\right]}{N_i} - r_i \left[f_{qi}\left(q_i,\dot{q}_i\right) + \rho_{fqi}sat\left(r_i,\epsilon_{ri}\right)\right] - r_i \left[\tau_{basei} + I_{mi}\rho_{base}sat\left(r_i,\epsilon_{ri}\right)\right] - \sum_{j=1}^4 \left\{r_i Y_{ij}\left(\dot{q}_i\right) \left[F_{ij}^v + \rho_{Fij}sat\left(r_i Y_{ij}\left(\dot{q}_i\right),\epsilon_{Fij}\right)\right]\right\}$$

$$(6.19)$$

where F_{ij}^{v} and ρ_{Fij} are the j_{th} element of F_{i}^{v} and ρ_{Fi} , respectively.

From Assumptions 7–10, if $|r_i| > \epsilon_{ri}$, the second to fifth items in Eq.(6.18) are negative, i.e.,

$$-r_{i}\left[\tilde{f}_{i}\left(\dot{q}_{i}\right) + \rho_{fi} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] < 0$$

$$-\frac{1}{N_{i}} \cdot r_{i}\left[\tilde{\tau}_{ti} + \rho_{\tau ti} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] < 0$$

$$-r_{i}\left[f_{qi}\left(q_{i},\dot{q}_{i}\right) + \rho_{fqi}sat\left(r_{i},\epsilon_{ri}\right)\right] < 0$$

$$-r_{i}\left[\tau_{basei} + I_{mi}\rho_{base} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] < 0$$
(6.20)

If $|r_i| \leq \epsilon_{ri}$, we have

$$-r_{i}\left[\check{f}_{i}\left(\dot{q}_{i}\right) + \rho_{fi} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] \leq \rho_{fi} r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}$$

$$-\frac{1}{N_{i}} \cdot r_{i}\left[\tilde{\tau}_{ti} + \rho_{\tau ti} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] \leq \frac{\rho_{\tau ti}}{N_{i}}r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}$$

$$-r_{i}\left[f_{qi}\left(q_{i},\dot{q}_{i}\right) + \rho_{fqi}sat\left(r_{i},\epsilon_{ri}\right)\right] \leq \rho_{fqi}r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}$$

$$-r_{i}\left[\tau_{basei} + I_{mi}\rho_{base} \cdot sat\left(r_{i},\epsilon_{ri}\right)\right] \leq I_{mi}\rho_{base}r_{i}\left\{\frac{r_{i}}{|r_{i}|} - \frac{r_{i}}{\epsilon_{ri}}\right\}$$

$$(6.21)$$

Similarly, from Property 2, if $|r_iY_{ij}(\dot{q}_i)| > \epsilon_{Fij}$, the last item in Eq.(6.19) satisfies

$$-r_i Y_{ij} \left(\dot{q}_i \right) \left[F_{ij}^v + \rho_{Fij} sat \left(r_i Y_{ij} \left(\dot{q}_i \right), \epsilon_{Fij} \right) \right] < 0$$
(6.22)

If $|r_i Y_{ij}(\dot{q}_i)| \leq \epsilon_{Fij}$, we have

$$-r_{i}Y_{ij}\left(\dot{q}_{i}\right)\left[F_{ij}^{v}+\rho_{Fij}sat\left(r_{i}Y_{ij}\left(\dot{q}_{i}\right),\epsilon_{Fij}\right)\right]$$

$$\leq\rho_{Fij}r_{i}Y_{ij}\left(\dot{q}_{i}\right)\left\{\frac{r_{i}Y_{ij}\left(\dot{q}_{i}\right)}{\left|r_{i}Y_{ij}\left(\dot{q}_{i}\right)\right|}-\frac{r_{i}Y_{ij}\left(\dot{q}_{i}\right)}{\epsilon_{Fij}}\right\}$$
(6.23)

Since the right-side terms of Eq.(6.21) and Eq.(6.22) achieve the maximum values at $|r_i| = \frac{\epsilon_{ri}}{2}$ and $|r_iY_{ij}(\dot{q}_i)| = \frac{\epsilon_{Fij}}{2}$, respectively, we can obtain,

$$\dot{V} \leq -I_{mi}N_i\lambda_i r_i^2 + \sum_{j=1}^4 \frac{\rho_{Fij}\epsilon_{Fij}}{4} + \frac{\epsilon_{ri}}{4} \left(\rho_{fi} + \frac{\rho_{\tau ti}}{N_i} + \rho_{fqi} + I_{mi}\rho_{base}\right)$$
(6.24)

From Eq.(6.24), V is a Lyapunov function only when

$$|r_i| > \sqrt{\frac{\frac{\epsilon_{ri}}{4} \left(\rho_{fi} + \frac{\rho_{\tau ti}}{N_i} + \rho_{fqi} + I_{mi}\rho_{base}\right) + \sum_{j=1}^{4} \frac{\rho_{Fij}\epsilon_{Fij}}{4}}{I_{mi}N_i\lambda_i}}$$
(6.25)

 $Define \ S = \left\{ r_i \in \Re \left| r_i^2 \le \frac{\frac{\epsilon_{ri} \left(\rho_{fi} + \frac{\rho_{\tau ti}}{N_i} + \rho_{fqi} + I_{mi} \rho_{base} \right)}{2} + \sum_{j=1}^{4} \frac{\rho_{fij} \epsilon_{Fij}}{2}}{I_{mi} N_i \lambda_i} \right\}, \ on \ the \ surface \ of \ S, \ \partial S, \ we \ have$

$$\dot{V} \le -\left\{\frac{\epsilon_{ri}}{4}\left(\rho_{fi} + \frac{\rho_{\tau ti}}{N_i} + \rho_{fqi} + I_{mi}\rho_{base}\right) + \sum_{j=1}^4 \frac{\rho_{Fij}\epsilon_{Fij}}{4}\right\}$$
(6.26)

Denote t_s as the time for the solution trajectory to intersect the surface ∂S , then

$$t_{s} \leq \frac{V(r_{i}(0)) - V(r_{i}(t_{s}))}{\frac{\epsilon_{ri}}{4} \left(\rho_{fi} + \frac{\rho_{\tau ti}}{N_{i}} + \rho_{fqi} + I_{mi}\rho_{base}\right) + \sum_{j=1}^{4} \frac{\rho_{Fij}\epsilon_{Fij}}{4}}$$
(6.27)

Therefore, r_i is bounded, which indicates that e_i and \dot{e}_i are bounded as per the proof in (Slotine and Li 1991).

6.2 Interactive Force Compensation in Passive Mode

The proposed interactive force compensation technique is to make the wrist move freely without generating excessive internal force. When a joint that is equipped with a mechanical clutch works in passive mode, the joint is totally free and will not generate any internal force. When a rope is used to pull a door open, it will not generate any internal forces that resist motion along the pitch or yaw direction. Similarly, if the wrist-environment interactive forces, which can be measured by the force/torque sensor, are controlled to be around zero, the compact wrist will work in a passive mode, generating little resistance force. It should be noted that the friction at the motor and transmission systems tends to prevent the compact wrist from moving freely. Thus, friction compensation is essential to enable the wrist working in a free passive mode. The Jacobian matrix J shown in Equation Eq.(6.2) is singular at $\delta = 0$, $\gamma = 0$. At this point τ_{t1} , τ_{t2} will always equal to zero, thus the joint space passive control will not work. In passive mode, this singular point is not avoidable, as a result, we need to find another control algorithm for the passive mode.

Let the force exerted by the gripper on a compliant environment be f(t). If the gripper has a linear compliance of K_r , and the compliant environment in contact with gripper has a linear compliance K_e . Then the wrist and environment combination has an aggregate compliance of $K_t = K_r + K_e$ and the gripper force at equilibrium is:

$$f(t) = K_t X(t) \tag{6.28}$$

The wrist is position controlled with control inputs of δ_d , γ_d . As an approximation, we neglect the position tracking error, i.e.,

$$\begin{aligned} x(t) &= x_d(t) \\ \dot{x}(t) &= \dot{x}_d(t) \end{aligned} \tag{6.29}$$

where

$$x(t) = \begin{bmatrix} \delta \\ \gamma \end{bmatrix}$$
(6.30)

Given a constant desired force f_d , the control task is to ensure that the force tracking error

 $\triangle f(t) = f(t) - f_d$, converges asymptotically to zero.

$$\lim_{t \to \inf} f(t) = 0 \tag{6.31}$$

where $\Delta f(t) = f(t) - f_d$ and $\Delta \dot{f}(t) = \dot{f}(t)$. If the interaction force f(t) and the plant state x(t) and $\dot{x}(t)$ are measurable, it is easy to show that the control law of

$$\dot{x}_d(t) = K_c \triangle f(t) \tag{6.32}$$

results in an exponentially stable first order close-loop force dynamic of

$$\Delta f(t) = -K_c K_t \Delta f(t) \tag{6.33}$$

Note that the control law requires neither the differentiation of a force signal, nor the knowledge of the robot or environment compliance parameters. If we let $f_d = 0$, then it becomes a passive mode control algorithm.

6.3 Control System Design

To verify the developed algorithms and to validate the proposed design, a DSP based control system was developed for multiple mode control of the compact wrist, as detailed in the subsection for experimental setup.

The control system diagram is as shown in Fig. 6.3. The DSP used in this control system is TMS320F2812 made by Texas Instruments, which is a 32-bit digital signal controller with flash. Details on this DSP can be found from the data manual (SPRS174T 2012). The Mini45-ERA transducer (ATI Industrial Automation,Inc. 2012), made by ATI Industrial Automation, was selected as the force/torque sensor. The Mini45-ERA transducer uses six half-bridge strain gauge pairs to sense loads. The equivalent electrical schematic of the transducer is shown in Fig. 6.3. The signal conditioning circuit was developed on the basis of AD8221, a gain programmable, high performance instrumentation amplifier. The AD8221 maintains a high CMRR over frequency, which allows it to reject wide band interference and line harmonics, greatly simplifying filter requirements. In the developed signal conditioning circuit, the strain gauge outputs, "SG0, SG1 \cdots SG5" shown in Fig. 6.3(a), are connected to "+IN", as shown



Figure 6.2: The control system diagram

in Fig. 6.3(b). From Fig. 6.3(b), the transfer function for the *AD*8221 can be given by

$$V_{out} = V_{ref} + G \left(V_{IN+} - V_{IN-} \right) \tag{6.34}$$

where G is the gain of the amplifier.

Furthermore, the force/torque measurements can be determined as

$$\begin{bmatrix} F_x \\ F_y \\ F_z \\ \tau_x \\ \tau_y \\ \tau_z \end{bmatrix} = M \cdot \begin{bmatrix} SG_0 \\ SG_1 \\ SG_2 \\ SG_3 \\ SG_4 \\ SG_5 \end{bmatrix}$$
(6.35)

where $SG_i = V_{outi} - V_{refi}$; and M is the decoupling matrix of the sensor.

The developed electronic control board is as shown in Fig. 6.4. Fig. 6.4(a) and 6.4(b) give the front side and back side of the board, respectively. The developed board is light and small, and can be mounted at the end of the link, as shown in Figs. 6.5(a) and Fig. 6.5(b). In the experiments to be described in the following subsections, the sampling time was selected as 4 milliseconds.



Figure 6.3: Development of signal conditioning circuit: (a) equivalent electrical schematic for the transducer; (b) designed signal conditioning circuit



Figure 6.4: The electronic control board: (a) front side; (b) back side.



Figure 6.5: The board mounted inside the link
6.4 Experiments

To verify the developed algorithms and to validate the proposed design, a DSP based control system was developed for multiple mode control of the compact wrist, as detailed in the subsection for experimental setup. Several experiments have been conducted, and the experimental results were reported in the following subsections. The first experiment was designed to verify the developed robust adaptive motion tracking controller with the compact wrist working in active mode; the second experiment was conducted to validate the wrist-environment interactive force compensation technique with the compact wrist working in passive mode; and the last experiment demonstrates the application of the developed algorithms to door opening.

6.4.1 Experimental Setup

Maxon DC motors were selected to drive the compact wrist, and the Maxon planetary gear heads GP32A (gear ratio 531:1) were used as speed reducers. The gear boxes were customized spur gears with the reduction ratio of 2:1. HEDL-5540A02 optical encoders were used for measuring the wrist's joint space motion.

This experiment is designed to verify the robust adaptive controller that is developed for tracking control of the compact wrist with active working mode. The experimental setup is as shown in Fig. 6.5(a); and the design parameters and control parameters are detailed as shown in Table 6.1.

Remark 3 As the first-version prototype, the compact wrist developed in our lab has the range of motion as follows: $-30^{\circ} < \delta, \gamma < 30^{\circ}$. Furthermore, to keep the compactness and the lightweight of the wrist, the wrist was designed with high gear ratio, which is 531 : 1. As a result, the wrist cannot work at very high speeds. To avoid damaging the wrist, the experiments conducted in the following subsections were designed to guarantee that the physical limits were not surpassed. While having limited range of motion and task-space velocities, the wrist prototype can be used to validate the developed control algorithms, which are general and can be extended to control other wrists.

Design and control parameters				Uncertainty bounds	
I_{m1}	$10.5\times10^{-4}gm^2$	ϵ_{Fi1}	10^{-4}	$ ho_{Fi1}$	10^{-3} (Nms/rad)
I_{m2}	$10.5\times10^{-4}gm^2$	ϵ_{Fi2}	10^{-3}	$ ho_{Fi2}$	10^{-2} (Nm)
k_{Ii}	10.0	ϵ_{Fi3}	10^{-3}	$ ho_{Fi3}$	10^{-2} (Nm)
N_i	531	ϵ_{Fi4}	0.10	$ ho_{Fi4}$	1.0 (s^2/rad^2)
λ_i	160	$\epsilon_{\dot{q}_i}$	0.01	$ ho_{fqi}$	0.5 (Nm)
μ_{Fic}	0.10	ϵ_{ri}	0.10	$ \rho_{\tau ti} $	1.0 (Nm)

 Table 6.1: Design parameters and control parameters

6.4.2 Experiments on Tracking Control with Active Mode

The wrist as shown in Fig. 6.6 is controlled to follow the task space trajectory given by Fig. 6.7. The experimental results are shown in Fig. 6.8 to Fig. 6.11. The joint space trajectory and velocities derived from the inverse kinematics and differential kinematics are shown in Fig. 6.8 and Fig. 6.9, respectively. Fig. 6.10 gives the tracking errors in task space; and the tracking velocity errors are shown in Fig. 6.11. From these figures, we can see that the developed active mode control algorithm is effective to control the compact wrist to follow the desired pitch and yaw rotations.

6.4.3 Experiments on Force Compensation with Passive Mode

In the last subsection, experiments are conducted to verify the active motion control mode. In this subsection, experiments are designed to validate the developed interactive force compensation algorithm, which enables the wrist working in passive mode. The control parameters for the interactive force compensation controller are selected as shown in Table 6.1, and $K_c = 0.1$. The experiments are conducted for two different cases. In *Case 1*, the DC motors are disabled. In *Case 2*, the wrist is controlled with the interactive force compensation algorithm developed in this paper. For both cases, the output link of the wrist is pushed by a human finger along two different directions, as shown in Fig. 6.12.

In *Case 1*, the wrist does not move even when more than 10Nm pitch torque is generated at the force/torque sensor mounting point, as shown in Fig. 6.13 and Fig. 6.15. The experimental



Figure 6.6: a snapshot for tracking control in active mode



Figure 6.7: The desired task-space trajectory in active mode



Figure 6.8: The calculated joint-space trajectory



Figure 6.9: The calculated joint-space velocities



Figure 6.10: The position tracking errors



Figure 6.11: The velocity tracking errors



(a)

(b)



Figure 6.12: Snapshots for the compact wrist working in passive mode

results for *Case 1* demonstrates that friction compensation is essential to enable the wrist to work in passive mode; the frictional force, being enlarged by the speed reducer, is big enough to prevent the wrist from moving freely.



Figure 6.13: The interactive motions in *Case 1*



Figure 6.14: The interactive motions in *Case 2*



Figure 6.15: The internal forces generated in Case 1

In *Case 2*, the wrist can move freely with a small force exerted by a finger. The interactive motions and internal forces in *Case 2* are as shown in Fig. 6.14 and Fig. 6.16, respectively. The compensation torques that generated by the motors are illustrated in Fig. 6.17. From the experimental results for *Case 2*, we can see that the developed interactive force compensation algorithm is effective to enable the wrist working in passive mode. The residual internal torques are less than 2Nm, which have been reduced dramatically compared to the case without control.

In practical applications, this small residual internal force is helpful to prevent the wrist from moving under small disturbance forces or force/torque sensor measurement noise.

Remark 4 The generated interactive forces are determined by the accelerations of the robot, *i.e.*, the change of velocities. If a sharp force is exerted to the end-effector within a very short period of time, a big shock force may be generated in the wrist, which should be avoided in practical applications to avoid damaging the wrist. On the other side, if the forces are exerted gradually, the motion speeds do not have extensive influences on the generated internal forces or the compensation torques.



Figure 6.16: The internal forces generated in Case 2



Figure 6.17: The compensation torques in Case 2

6.4.4 Application to Door Opening

As well known, slippage is almost unavoidable for a mobile manipulator tracking a curved trajectory, especially when the load distribution is time-varying due to the complicated interactions between the mobile platform and the on-board manipulator (Liu and Liu 2009). As a result, the conventional position control algorithms are not suitable for door opening because of the inaccurate tracking performance of the mobile platform. One important concern is that large internal forces may be generated, which will cause unnecessary wearing of mechanical parts. In this subsection, the developed compact wrist and the proposed multiple mode control algorithm are implemented for door opening, which have been verified to be able to relieve the potential internal forces effectively.

The compact wrist and force/torque sensor assembly developed in this paper is integrated with a 3-DOF modular reconfigurable manipulator that was developed in our lab (Liu et al. 2011); and the integrated manipulator is mounted on top of a *Powerbot* Automatic Guided Vehicle (AGV), a commercial mobile platform manufactured by *MobileRobots Inc*. The *Powerbot* AGV is differentially steered with the two fixed wheels mounted on each side of the robot, and two caster wheels are equipped to keep balancing of the robot. The integrated mobile manipulator is used to pull an artificial door open, as shown in Fig. 6.18(a).

The mobile platform is positioned in front of the "door", and the door knob is grasped manually. The modular reconfigurable manipulator consists of three rotary joints, i.e., Turret, Shoulder and Elbow joints, as shown in Fig. 6.18(a); and the joints are all equipped with torque sensors. To verify the developed multi-mode control algorithm, the Turret joint and the compact wrist are controlled with passive mode, and the Shoulder as well as the Elbow joints are locked to keep the same hight during door opening. The mobile platform is controlled to follow an almost circular trajectory, so as to pull the door open for ninety degrees. Snapshots for the door opening process are shown in Fig. 6.18.

The experimental results for door opening are presented in Fig. 6.19 and Fig. 6.20. Fig. 6.19 demonstrates the interactive motions of the wrist during the course of door opening. The wrist-knob interactive torques were measured as shown in Fig. 6.20. In the experiments, jerking and sliding of the mobile platform can be obviously observed, which may generate large internal forces in the on-board manipulator. With the proposed multiple control algorithm, the disturbances caused by mobile robot's jerking and sliding can be effectively accommodated and internal torques generated in the wrist can be limited to be less than 2 Nm.



(b)



Figure 6.18: Snapshots for door opening



Figure 6.19: Interactive motions of the wrist in door opening



Figure 6.20: The wrist-knob interactive torques in door-opening

To test the robustness of the developed internal force compensation algorithm with respect to accumulated positioning errors of the mobile platform, experiments were repeated with intentionally introduced initial heading angular errors. From the experimental results, the mobile manipulator with the compact wrist could open the door with measured internal torques that are still of comparable magnitude to the case in which no heading angular error was introduced. For example, the torque measurements at the wrist reached a maximum of 3 Nm when a 3-degree initial offset was introduced. To avoid unnecessary duplicate, experimental results with different initial heading angles are not detailed in this paper.

Remark 5 While applying the developed control algorithms to door opening, precise dimension of the door is not required. However, due to the limited range of motion of the developed wrist prototype, circular trajectory of the mobile platform was planned to be consistent with the nominal radius of the door so as to make sure that the wrist will work within its physical limits. The experimental results with obvious observation of jerking and sliding and the intentionally introduced initial heading angles have confirmed the robustness of the developed control algorithms with respect to door

Remark 6 In the experiments reported in this section, switching between active mode and passive mode were made manually. In practical applications, the switching can be enabled automatically based on the events that were defined in advance. For example, while grasping the knob, the robot needs to move at high accuracy and there is not any interactive forces exerted on the robot, active mode can be enabled. After the knob is grasped and during the course of door opening, excessive internal forces may be generated, and it is desirable to switch from active mode to passive mode. Another option for automatic mode switching is to set up a threshold for the measured wrist-environment interactive torques. As long as the the internal torques are large enough it will trigger the switching from active mode to passive mode to active mode can be triggered if the interactive torques drop below certain thresholds. On-line mode switching will be investigated in our future research works.

Chapter 7

Conclusion and Future Work

7.1 Conclusion

In uncontrolled environments, the robot has to adapt to the world consisting of only partially known or unknown objects and tasks, and real-time constraints. The capability of robots working in both active and passive modes and switching between them helps the robots to perform in unstructured environments. A typical modular and reconfigurable robot consists of general rotational joints as well as special joints with multiple degrees of freedom. This dissertation work has provided methods to control both kinds of joint modules to work in either active or passive modes.

For a general rotational joint with harmonic drive, a novel mathematical model for the compliance of harmonic drives has been proposed. When combined with a friction model, the proposed model captures the nonlinear stiffness and hysteresis phenomenon of the harmonic drive transmission. Numerical simulations and experiments have been conducted to test the proposed modeling method. The accurate match in the results confirmed the effectiveness of the proposed model. The advantages of the proposed model are multifold including its simple structure, its ability of capturing hysteresis, and easiness of integrating to control system. Furthermore, the proposed modeling approach does not require detailed knowledge of the gear tooth geometry or wave generator kinematics to account for hysteresis model as in other works. The model was compared with measured data while the shaft was locked or free. The proposed model resolves the problems in estimating harmonic drive model parameters associated with the previously proposed models and can predict the harmonic drive behaviour at operating points other than those used for model identification.

Based on the developed harmonic drive compliance model, a joint torque estimation method using position measurements is provided. The torque estimation based on position measurements provides an advantage of noise immunity to the estimated joint torque. Using the torsional compliance of harmonic drives instead of an additional elastic component does not change the joint dynamics. Moreover, adding a link-side position sensor has a potential to improve the joint control accuracy and to reduce the cost of joint torque sensing. The estimated torque can be used in robotic control algorithms with JTF and in collision detection/avoidance schemes. Using the developed torque estimation technique, a multiple working mode control algorithm for modular and reconfigurable robot using proposed torque estimation technique has been developed and experimentally tested.

For robot joints with multiple degrees of freedom, a compact wrist equipped with a multiple working mode control system has been developed and experimentally tested. While working in active mode, the developed robust adaptive controller does not rely on a priori dynamic model and can suppress uncertainties caused by sensor inaccuracies and noises. With the proposed interactive force compensation technique, the wrist can move freely without generating excessive internal force. The developed multiple mode control algorithm makes the compact wrist capable of working in sophisticated environments, such as door opening. A prototype wrist has also been developed and the experimental results verified the proposed multiple mode control algorithm.

7.2 Future Work

The development of modular and reconfigurable robot is a long-time work which requires much research including redesign work and improvements. A few directions for future work is discussed as follows.

The link side absolute position encoder used in the research has a 0.01 deg accuracy as provided by the manufacturer. However, the error is sometimes bigger than the accuracy provided by the manufacturer because of installation error etc., and we can not identify that the error is caused by sensor error or harmonic drive kinematic error. In this dissertation, we combined the sensor error with kinematic error. Given a higher accuracy position sensor to calibrate the absolute encoder in the link side, we can separate the sensor error with the harmonic drive kinematic error, and the kinematic error can be modeled with better accuracy.

The performance of multiple mode control highly depends on friction compensation especially when the robot joint works in passive mode. A general Coulomb and viscous model is used in this dissertation research. However, this model can not capture that the friction of harmonic drive relies on position. To complete the whole harmonic drive model and improve the performance of the robot working in passive mode, a more complete harmonic drive friction model should be developed.

The current experimental joint is controlled by a PC, and the algorithm is implemented in MATLAB/Simlink model. By developing a single board DSP controller for the HDT joint with an absolute encoder and an incremental encoder and a DC motor driver, and implementing the MATLAB/Simlink model into the DSP controller, one could develop a modular and reconfigurable robot joint based on the proposed torque estimation method, building a multiple joint robot to verify the proposed torque estimation technique and multiple working mode control algorithm. Furthermore, the effectiveness of the proposed torque estimation technique in collision detection can also be investigated.

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